

# Lecture Slides for Physics 1050

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## Skating

### Observations about Skating

- When you're at rest on a level surface,
  - without a push, you remain stationary
  - with a push, you start moving that direction
- When you're moving on a level surface,
  - without a push, you coast steady & straight
  - with a push, you change direction or speed

### 4 Questions about Skating

- Why does a stationary skater remain stationary?
- Why does a moving skater continue moving?
- Why does a skater need ice or wheels to skate?
- How does a skater start or stop moving?

### Question 1

- Why does a stationary skater remain stationary?
  - What keeps the dishes in place on a table?
  - If I pull the tablecloth, what will happen?
  - Does the speed at which I pull matter?

### Physics Concept

- **Inertia** (just the first part)
  - A body at rest tends to remain at rest

## Question 2

- Why does a moving skater continue moving?
  - What keeps a moving banana moving?
  - Can I slice a moving banana in midair?

## Physics Concept

- Inertia (the whole thing)
  - A body at rest tends to remain at rest
  - A body in motion tends to remain in motion

## Newton's First Law (Version 1)

- An object that is free of external influences moves in a straight line and covers equal distances in equal times.

## Question 3

- Why does a skater need ice or wheels to skate?
  - Why does a hovercraft need an air cushion?

## Keeping It Simple

- Real-world complications mask simple physics
- Solution: minimize or overwhelm complications
- To demonstrate inertia:
  - work on level ground (goodbye gravity)
  - use wheels, ice, or air support (goodbye friction)
  - work fast (overwhelm friction and air resistance)

## Physical Quantities

- Position – an object's location
- Velocity – its change in position with time

### **Newton's First Law (Version 2)**

- An object that is free of external influences moves at a constant velocity.

### **Physical Quantities**

- Position – an object's location
- Velocity – its change in position with time
- Force – a push or a pull

### **Newton's First Law**

- An object that is not subject to any outside forces moves at a constant velocity.

### **Question 4**

- How does a skater start or stop moving?
  - What does a push do?
  - What does a skater respond to a push?
  - Do all skaters respond equally to equal pushes?

### **Physical Quantities**

- Position – an object's location
- Velocity – change in position with time
- Force – a push or a pull
- Acceleration – change in velocity with time
- Mass – measure of object's inertia

### **Newton's Second Law**

- An object's acceleration is equal to the net force exert on it divided by its mass. That acceleration is in the same direction as the net force.

$$\text{acceleration} = \text{net force} / \text{mass}$$

$$\text{net force} = \text{mass} \cdot \text{acceleration}$$

## Summary about Skating

- Skates can free you from external forces
- When you experience no external forces,
  - You coast – you move at constant velocity
  - If you're at rest, you remain at rest
  - If you're moving, you move steadily and straight
- When you experience external forces
  - You accelerate – you move at a changing velocity
  - Acceleration depends on force and mass

## Falling Balls

### Observations about Falling Balls

- When you drop a ball, it
  - begins at rest, but acquires downward speed
  - covers more and more distance each second
- When you tossed a ball straight up, it
  - rises to a certain height
  - comes briefly to a stop
  - begins to descend, much like a dropped ball
- A thrown ball travels in an arc

### 5 Questions about Falling Balls

- Why does a dropped ball fall downward?
- Do different balls fall at different rates?
- Would a ball fall differently on the moon?
- Can a ball move upward and still be falling?
- Does a ball's horizontal motion affect its fall?

### Question 1

- Why does a dropped ball fall downward?
  - What is gravity doing to the ball?

### Gravity and Weight

- Gravity exerts a force on the ball
- That force is the ball's weight
- Since earth's gravity produces the ball's weight, that weight points toward the earth's center
- The ball's weight causes it to accelerate toward the earth's center (i.e., downward)

## Question 2

- Do different balls fall at different rates?
  - If different balls have different weights and different masses, is there any relationship between their accelerations as they fall?

## Weight and Mass

- A ball's weight is proportional to its mass  
 $\text{weight/mass} = \text{constant}$
- On earth's surface,  
 $\text{weight/mass} = 9.8 \text{ newtons/kilogram}$ 
  - is the same for all balls (or other objects)
  - is called "acceleration due to gravity"

## Acceleration Due to Gravity

- Why this strange name?  
 $\text{weight/mass} \rightarrow \text{force/mass} = \text{acceleration}$
- Acceleration due to gravity is an acceleration!  
 $9.8 \text{ newtons/kilogram} = 9.8 \text{ meter/second}^2$
- On earth's surface, all falling balls accelerate downward at  $9.8 \text{ meter/second}^2$
- Different balls fall at the same rate!

## Question 3

- Would a ball fall differently on the moon?
  - Yes!
  - Moon's acceleration due to gravity is different!

## Question 4

- Can a ball move upward and still be falling?
  - How does falling affect a ball's
    - acceleration?
    - velocity?
    - position?

## A Falling Ball (Part 1)

- A falling ball accelerates downward steadily
  - Its acceleration is constant and downward
  - Its velocity increases in the downward direction
- When falling from rest (stationary), its
  - velocity starts at zero and increases downward
  - altitude decreases at an ever faster rate

## Falling Downward

Position	Fall time	Velocity	Acceleration
0 m	0 s	0 m/s	$\downarrow -9.8 \text{ m/s}^2$
-4.9 m	1 s	$\downarrow -9.8 \text{ m/s}$	$\downarrow -9.8 \text{ m/s}^2$
-19.6 m	2 s	$\downarrow -19.6 \text{ m/s}$	$\downarrow -9.8 \text{ m/s}^2$
-44.1 m	3 s	$\downarrow -29.4 \text{ m/s}$	$\downarrow -9.8 \text{ m/s}^2$

## A Falling Ball (Part 2)

- A falling ball can start by heading upward!
  - Its velocity starts in the upward direction
  - Its velocity becomes less and less upward
  - Its altitude increases at an ever slower rate
  - At some point, its velocity is momentarily zero
  - Its velocity becomes more and more downward
  - Its altitude decreases at ever faster rate

## Falling Upward First

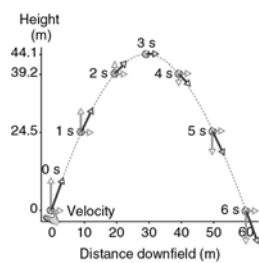
Position	Fall time	Velocity	Acceleration
44.1 m	3 s	0 m/s	$\downarrow 9.8 \text{ m/s}^2$
39.2 m	2 s	$\uparrow 9.8 \text{ m/s}$	$\downarrow 9.8 \text{ m/s}^2$
24.5 m	1 s	$\uparrow 19.6 \text{ m/s}$	$\downarrow 9.8 \text{ m/s}^2$
0 m	0 s	$\uparrow 29.4 \text{ m/s}$	$\downarrow 9.8 \text{ m/s}^2$

## Question 5

- Does a ball's horizontal motion affect its fall?
- Why does a thrown ball travel in an arc?

## Throws and Arcs

- Gravity only affects only the ball's vertical motion
- A ball coasts horizontally while falling vertically



## Summary About Falling Balls

- Without gravity, a free ball would coast
- With gravity, an otherwise free ball
  - experiences its weight,
  - accelerates downward,
  - and its velocity becomes increasingly downward
- Whether going up or down, it's still falling
- Its horizontal coasting motion is independent of its vertical falling motion

# Ramps

## Observations About Ramps

- It's difficult to lift a heavy cart straight up
- It's easier to push a heavy cart up a ramp
- The ease depends on the ramp's steepness
- Gradual ramps involve gentler pushes
- Gradual ramps involve longer distances

## 4 Questions about Ramps

- Why doesn't the cart fall through the ramp?
- Are the cart and ramp pushing on each other?
- Why is it easier to push the cart up a ramp?
- Is there a physical quantity that's the same for any trip up the ramp, regardless of its steepness?

## Question 1

- Why doesn't the cart fall through the ramp?
  - Why doesn't a ball fall through a table?
  - Is the table pushing up on the ball?
  - How can an upward push prevent falling?

## Support Forces

- A support force
  - prevents the ball from penetrating the table's surface
  - points directly away from the table's surface
- Forces along surface are friction (*ignore for now*)

## Adding up the Forces

- As it sits on the table, the ball experiences
  - its weight downward
  - a support from the table upward
- Since the ball isn't accelerating,
  - the sum of forces (the net force) on the ball is zero
  - so the support force must balance ball's weight!
- Since cart isn't accelerating into ramp,
  - the ramp's support force must keep cart on surface

## Question 2

- Are the cart and ramp pushing on each other?
- Are the ball and table pushing on each other?
  - Is the table pushing on the ball?
  - Is the ball pushing on the table?
  - Which is pushing harder?

## Newton's Third Law

- For every force that one object exerts on a second object, there is an equal but oppositely directed force that the second object exerts on the first object.

## Forces Present (Part 1)

- For the ball resting on the table, the forces are
  1. On ball due to gravity (its weight) } zero
  2. On ball due to support from table } acceleration
  3. On table due to support from ball } pair
- These forces all have the same magnitude
- Where is the other 3<sup>rd</sup> law pair?

## Forces Present (Part 2)

1. On earth due to gravity from the ball } 3<sup>rd</sup> law
  2. On ball due to gravity from the earth } pair
  3. On ball due to support from table } 3<sup>rd</sup> law
  4. On table due to support from ball } pair
- Forces 2 and 3 aren't a Newton's 3<sup>rd</sup> law pair!
    - when equal in magnitude, ball doesn't accelerate
    - when not equal in magnitude, ball accelerates!

## Misconception Alert

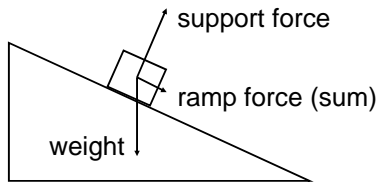
- While the forces two objects exert on one another must be equal and opposite, the net force on each object can be anything.
- Each force within an equal-but-opposite pair is exerted on a different object, so they don't cancel directly.

## Question 3

- Why is it easier to push the cart up a ramp?
  - Why does the ramp's steepness matter?
  - Why does the cart tend to roll downhill?



## Forces on a Cart on a Ramp



- Ramp force causes cart to accelerate downhill

## Balanced Cart on Ramp

- If you balance the ramp force,
  - the net force on the cart will be zero,
  - the cart won't accelerate,
  - and it will coast uphill or downhill or remain at rest
- The more gradual the ramp,
  - the more nearly its weight and the support balance,
  - the smaller the ramp force on the cart,
  - and the easier it is to balance the ramp force!

## Question 4

- Is there a physical quantity that's the same for any trip up the ramp, regardless of its steepness?
- What physical quantity is the same for
  - a long trip up a gradual ramp
  - a medium trip up a steep ramp
  - a short trip straight up a vertical ramp

## Energy and Work

- Energy – a conserved quantity
  - it can't be created or destroyed
  - it can be transformed or transferred between objects
  - is the capacity to do work
- Work – mechanical means of transferring energy
$$\text{work} = \text{force} \cdot \text{distance}$$
(where force and distance in same direction)

## Work Lifting a Cart

- Going straight up: Force is large, Distance is small
$$\text{work} = \text{Force} \cdot \text{Distance}$$
- Going up ramp: Force is small, Distance is large
$$\text{work} = \text{Force} \cdot \text{Distance}$$
- The work is the same, either way!

## Mechanical Advantage

- Mechanical advantage:
  - Doing the same amount of work, but altering the balance between force and distance
- A ramp provides mechanical advantage
  - You can raise a heavy cart with a modest force,
  - but you must push that cart a long distance.
  - Your work is independent of the ramp's steepness

## The Transfer of Energy

- Energy has two principal forms
  - Kinetic energy – energy of motion
  - Potential energy – energy stored in forces
- Your work transfers energy from you to the cart
  - You do work on the cart
  - Your chemical potential energy decreases
  - The cart's gravitational potential energy increases

## Summary about Ramps

- Ramp supports most of the cart's weight
- You can easily balance the ramp force
- You do work pushing the cart up the ramp
- Your work is independent of ramp's steepness
- The ramp provides mechanical advantage
  - It allows you to push less hard
  - but you must push for a longer distance

## Wind Turbines

### Observations about Wind Turbines

- Wind turbines are symmetrical and balanced
- A balanced wind turbine rotates smoothly
- An unbalanced turbine settles heavy-side down
- Most wind turbines have three blades
- Wind turbines start or stop spinning gradually
- Wind turbines extract energy from the wind and convert it into electrical energy

### 6 Questions about Wind Turbines

- How does a balanced wind turbine move?
- Why does the wind turbine need a pivot?
- Why does a one-blade turbine spin unevenly?
- Why do blade weights and orientations matter?
- Why do giant turbines start and stop so slowly?
- How does energy go from wind to generator?

### Question 1

- How does a balanced wind turbine move?
  - Is a balanced wind turbine horizontal?
  - Is a horizontal wind turbine balanced?

## Physics Concept

- Rotational Inertia
  - A body at rest tends to remain at rest
  - A body that's rotating tends to keep rotating

## Physical Quantities

- Angular Position
  - an object's orientation
- Angular Velocity
  - change in angular position with time
- Torque – a twist or spin

## Newton's First Law of Rotational Motion

- A rigid object that's not wobbling and that is free of outside torques rotates at a constant angular velocity.

## Balanced Wind Turbine

- All by itself, a balanced wind turbine
  - experiences zero net torque
  - has a constant angular velocity
- Its angular velocity is constant when it is
  - motionless and horizontal
  - motionless and tilted
  - turning steadily in any direction

## Question 2

- Why does the wind turbine need a pivot?
  - How would a pivotless wind turbine move?

## Center of Mass

- The point about which an object naturally spins
- A free object rotates about its center of mass while its center of mass follows the path of a falling object

### Wind Turbine's Pivot

- The wind turbine needs a pivot to
  - support the weight of the turbine
  - prevent the turbine from falling
  - permit the turbine to rotate but not translate
- Placing the pivot at turbine's center of mass
  - allows the turbine to spin about its natural pivot
  - minimizes the forces required of the pivot

### Question 3

- Why does a one-blade turbine spin unevenly?
  - How does a torque affect a wind turbine?
  - How does gravity exert a torque on the turbine?

### Physical Quantities

- Angular Position
  - an object's orientation
- Angular Velocity
  - change in angular position with time
- Torque – a twist or spin
- Angular Acceleration
  - change in angular velocity with time
- Rotational Mass – measure of rotational inertia

### Newton's Second Law of Rotational Motion

- An object's angular acceleration is equal to the net torque exerted on it divided by its rotational mass. The angular acceleration is in the same direction as the torque.

$$\text{angular acceleration} = \text{net torque} / \text{rotational mass}$$

$$\text{net torque} = \text{rotational mass} \cdot \text{angular acceleration}$$

### Forces and Torques

- A force can produce a torque
- A torque can produce a force

$$\text{torque} = \text{lever arm} \cdot \text{force}$$

(where the lever arm is perpendicular to the force)

### A One-Blade Turbine's Uneven Rotation

- Blade's weight produces a torque on the turbine
  - Turbine undergoes angular acceleration
  - so turbine's angular velocity changes
- Direction of gravitational torque
  - reverses every half-turn
  - so turbine's angular speed fluctuates as it spins

### Question 4

- Why do the blades' weights and spacing matter?
  - Why are most wind turbines so symmetrical?

### Net Torque

- The net torque on the wind turbine is
  - the sum of all torques on the wind turbine
  - responsible for the turbine's angular acceleration
- If net torque is zero, angular velocity is constant

### Balancing the Blades

- Each blade experiences a gravitational torque
  - Left blade has ccw torque (weight · lever arm)
  - Right blade has cw torque (weight · lever arm)
- If those torques sum to zero,
  - turbine experiences zero gravitational torque
  - turbine is balanced

### Center of Gravity

- Wind turbine's center of gravity
  - is the effective location of the turbine's weight
  - coincides with the turbine's center of mass
- When turbine's center of gravity is at its pivot,
  - it experiences zero gravitational torque
  - it is balanced
- A symmetrical three-blade turbine is balanced

### Question 5

- Why do giant turbines start and stop so slowly?
  - How does blade length affect wind torque?
  - How does blade length affect rotational mass?

### A Blade's Wind Torque

- A blade's wind torque is proportional to
  - the wind's force on the blade
  - the blade's effective lever arm
- Doubling the length of a blade
  - increases its wind force by a factor of 2
  - increases its effective lever arm by a factor of 2
  - increases its wind torque by a factor of 4

### **A Blade's Rotational Mass**

- A blade's rotational mass is proportional to
  - the blade's mass
  - the square of blade's effective lever arm
- Doubling the length of a blade
  - increases its mass by a factor of 2
  - increases its lever arm by a factor of 2
  - increases its rotational mass by a factor of 8!

### **Turbine Size and Responsiveness**

- A wind turbine blade's
  - wind torque increases in proportion to its length<sup>2</sup>
  - rotational mass increases in proportion to its length<sup>3</sup>
- The larger the wind turbine,
  - the slower its angular accelerations
  - the longer it takes to start or stop turning

### **Question 6**

- How does energy go from wind to generator?
  - How does a rotating system do work?

### **Rotational Work**

- Wind does translational work on a turbine blade:
  - wind exerts a force on blade
  - blade moves a distance in direction of that force
  - so energy moves from wind to wind turbine
- Turbine does rotational work on a generator
  - turbine exerts a torque on generator
  - generator turns an angle in direction of that torque
  - so energy moves from wind turbine to generator

### **Summary about Wind Turbines**

- Without air or generator, balanced wind turbine
  - experiences zero gravitational torque
  - rotates at constant angular velocity
- Wind forces produce torques on turbine's blades
- Generator exerts opposing torque on turbine
- Wind turbine turns at constant angular velocity
- Energy goes from wind to turbine to generator

### **Wheels**

## Observations about Wheels

- Friction makes wheel-less objects skid to a stop
- Friction wastes energy
- Wheels mitigate the effects of friction
- Wheels can also propel vehicles

## 5 Questions about Wheels

- Why does a wagon need wheels?
- Why do sleds seem to “break free” and then slide easily when you shove them hard enough?
- What happens to energy as a sled skids to rest?
- How do wheels help a wagon coast?
- What energy does a wheel have?

## Question 1

- Why does a wagon need wheels?
- Why do sleds work well only on snow or ice?

## Frictional Forces

- A frictional force
  - opposes relative sliding motion of two surfaces
  - points along the surfaces
  - acts to bring the two surfaces to one velocity
- Frictional forces always come in 3<sup>rd</sup> law pairs:
  - Pavement’s frictional force pushes cart backward
  - Cart’s frictional force pushes pavement forward

## The Two Types of Friction

- Static Friction
  - Acts to prevent objects from starting to slide
  - Forces can range from zero to an upper limit
- Sliding Friction
  - Acts to stop objects that are already sliding
  - Forces have a fixed magnitude

## Question 2

- Why do sleds seem to “break free” and then slide easily when you shove them hard enough?

## Frictional Forces

- Frictional forces increase when you:
  - push the surfaces more tightly together
  - roughen the surfaces
- Peak static force is greater than sliding force
  - Surface features can interpenetrate better
  - Friction force drops when sliding begins

## Sleds and Friction

- A stationary sled
  - experiences static friction
  - won't start moving until you pull very hard
- A moving sled
  - experiences sliding friction
  - needs to be pulled or it will slow down and stop
  - experiences wear as it skids along the pavement

## Question 3

- What happens to energy as a sled skids to rest?

## Friction, Energy, and Wear

- Static friction
  - Both surfaces travel the same distance (often zero)
  - No work “disappears” and there is no wear
- Sliding friction
  - The two surfaces travel different distances
  - Some work “disappears” and becomes thermal energy
  - The surfaces experience wear
- A sliding box turns energy into thermal energy

## The Many Forms of Energy

- Kinetic: energy of motion
- Potential: stored in forces between objects
  - Gravitational
  - Elastic
  - Magnetic
  - Electric
  - Electrochemical
  - Chemical
  - Nuclear
- Thermal energy: the same forms of energy, but divided up into countless tiny fragments

## Energy and Order

- A portion of energy can be
  - Organized – ordered energy (e.g. work)
  - Fragmented – disordered energy (e.g. thermal energy)
- Turning ordered energy into disordered energy
  - is easy to do
  - is statistically likely
- Turning disordered energy into ordered energy
  - is hard to do
  - is statistically unlikely (it's effectively impossible)

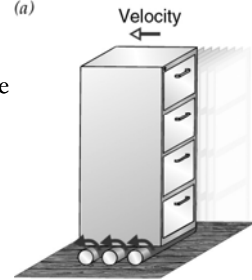


### Question 4

- How do wheels help a wagon coast?

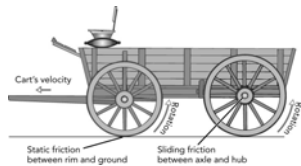
### Rollers

- Eliminate sliding friction <sup>(a)</sup> at roadway
- Are inconvenient because they keep popping out from under the object



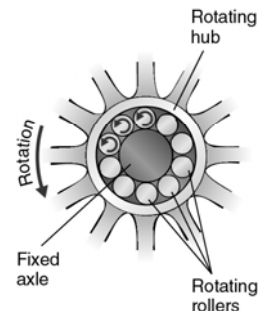
### Wheels

- Eliminate sliding friction at roadway
- Convenient because they don't pop out
- Allow static friction to exert torques on wheels and forces on vehicle
- Wheel hubs still have sliding friction



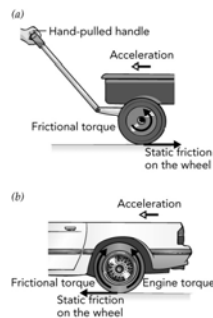
### Bearings

- Eliminate sliding friction in wheel hub
- Behave like automatically recycling rollers



### Practical Wheels

- Free wheels are turned by the vehicle's motion
- Powered wheels propel the vehicle as they turn.



### Question 5

- What energy does a wheel have?

## Wheels and Kinetic Energy

- A moving wheel has kinetic energy:  
kinetic energy =  $\frac{1}{2} \cdot \text{mass} \cdot \text{speed}^2$
- A spinning wheel has kinetic energy:  
kinetic energy =  $\frac{1}{2} \cdot \text{rotational mass} \cdot \text{ang. speed}^2$
- A moving and spinning wheel has both
- Both kinetic energies are transferred via work

## Summary about Wheels

- Sliding friction wastes energy
  - Wheels eliminate sliding friction
  - A vehicle with wheels coasts well
- Free wheels are turned by static friction
- Powered wheels use static friction to propel car

## Bumper Cars

### Observations about Bumper Cars

- Moving cars tend to stay moving
- Changing a car's motion takes time
- Impacts alter velocities and angular velocities
- Cars often appear to exchange their motions
- The fullest cars are the hardest to redirect
- The least-full cars get slammed during collisions

### 3 Questions about Bumper Cars

- Does a moving bumper car carry a "force"?
- Does a spinning bumper car carry a "torque"?
- On an uneven floor, which way does a bumper car accelerate?

### Question 1

- Does a moving bumper car carry a "force"?
- Starting and stopping a bumper car seems to require the "investment" and "withdrawal" of some directed quantity of motion. What is it?

## Momentum

- A translating bumper car carries momentum
- Momentum
  - is a conserved quantity (can't create or destroy)
  - is a directed (vector) quantity
  - measures the translational investment the object needed to reach its present velocity  
 $\text{momentum} = \text{mass} \cdot \text{velocity}$

## Exchanging Momentum

- Bumper cars exchange momentum via impulses
- An impulse is
  - the only way to transfer momentum
  - a directed (vector) quantity  
 $\text{impulse} = \text{force} \cdot \text{time}$
- When  $\text{car}_1$  gives an impulse to  $\text{car}_2$ ,  $\text{car}_2$  gives an equal but oppositely directed impulse to  $\text{car}_1$ .

## Head-On Collisions

- Bumper cars exchange momentum via impulses
- The total momentum never changes
- Car with the least mass changes velocity most
- The littlest riders get creamed

## Question 2

- Does a spinning bumper car carry a “torque”?
- Spinning and un-spinning a bumper car seems to require the “investment” and “withdrawal” of some directed quantity of rotational motion. What is it?

## Angular Momentum

- A spinning car carries angular momentum
- Angular momentum
  - is a conserved quantity (can't create or destroy)
  - is a directed (vector) quantity
  - measures the rotational investment the object needed to reach its present angular velocity  
 $\text{angular momentum} = \text{rotational mass} \cdot \text{angular velocity}$

## Newton's Third Law of Rotational Motion

- For every torque that one object exerts on a second object, there is an equal but oppositely directed torque that the second object exerts on the first object.

## Exchanging Angular Momentum

- Bumper cars exchange angular momentum via angular impulses
- An angular impulse is
  - the only way to transfer angular momentum
  - a directed (vector) quantity
    - angular impulse = torque · time
- When car<sub>1</sub> gives an angular impulse to car<sub>2</sub>, car<sub>2</sub> gives an equal but oppositely directed angular impulse to car<sub>1</sub>.

## Glancing Collisions

- Bumper cars exchange angular momentum via angular impulses
- Total angular momentum about a specific inertial point in space remains unchanged
- Bumper car with the smallest rotational mass about that point changes angular velocity most
- The littlest riders tend to get spun wildly

## Rotational Mass can Change

- Mass can't change, so the only way an object's velocity can change is if its momentum changes
- Rotational mass can change, so an object that changes shape can change its angular velocity without changing its angular momentum

## Question 3

- On an uneven floor, which way does a bumper car accelerate?

## Potential Energy, Acceleration, and Force

- An object accelerates in the direction that reduces its total potential energy as rapidly as possible
- Forces and potential energies are related!
- A car on an uneven floor accelerates in whatever direction reduces its total potential energy as rapidly as possible

## Summary about Bumper Cars

- During collisions, bumper cars exchange
  - momentum via impulses
  - angular momentum via angular impulses
- Collisions have less effect on
  - cars with large masses
  - cars with large rotational masses

## Spring Scales

### Observations about Spring Scales

- They move downward during weighing
- They take a little time to settle
- They're only accurate when everything is at rest

### 4 Questions about Spring Scales

- What exactly is a spring scale measuring?
- How does a spring scale measure weight?
- What is the scale's dial or meter reporting?
- Why must you stand still on a spring scale?

### Question 1

- What exactly is a spring scale measuring?
- Are all measures of quantity equivalent?

### Mass as a Measure

- Pros:
  - Independent of measuring location
  - Can be measured directly:
    - Exert a known force
    - Measure the resulting acceleration
- Cons:
  - Measuring acceleration accurately is difficult

### Weight as a Measure

- Pros:
  - Proportional to mass
  - Measuring weight is easy
- Cons:
  - Dependent on measuring location
  - Can't be measured directly
- Spring scales measure weight, not mass

## Question 2

- How does a spring scale measure weight?

## Equilibrium

- Spring scales measure weight using equilibrium
- An object in equilibrium
  - experiences zero net force
  - is not accelerating
- At equilibrium,
  - individual forces sum to zero (they cancel perfectly).
  - an object at rest remains at rest
  - an object in motion coasts

## Weighing via Equilibrium

- Balance the object's weight with a support force
- Attain equilibrium
  - $\text{weight} + \text{support force} = 0$
- Measure the support force

## Question 3

- What is the scale's dial or meter reporting?
- How do you measure a support force?

## Springs

- When free, a spring adopts its equilibrium length
  - Its ends experience zero net force
  - Its ends are in equilibrium
- When distorted, its ends experience forces that
  - act to restore the spring to its equilibrium length
  - make the equilibrium length "stable"
  - are proportional to the distortion
  - are called "restoring forces"

## Hooke's Law

- The restoring force on the end of a spring is equal to a spring constant times the distance the spring is distorted. That force is directed opposite the distortion.

$$\text{restoring force} = - \text{spring constant} \cdot \text{distortion}$$

## A Spring Scale

- To weigh an object with a spring scale,
  - support the object with a spring,
  - allow the object to settle at equilibrium,
  - and measure the distortion of the spring.
- The spring constant relates distortion to force
- With proper calibration, reporting the spring's distortion is equivalent to reporting the restoring force that is supporting the object

## Question 4

- Why must you stand still on a spring scale?
- Why does the reading bounce briefly?

## Spring Scales and Acceleration

- Weight measurements require equilibrium
- Without equilibrium,
  - the spring force doesn't balance the weight
  - the "measurement" is meaningless
- Since an accelerating object is not at equilibrium,
  - you mustn't bounce on a scale!
  - you must wait for the scale to settle before reading!

## Oscillation

- When you first load a scale, it bounces
  - It accelerates toward a new equilibrium
  - It then coasts through that equilibrium
  - It then accelerates back toward the new equilibrium
  - It returns and overshoots many times
- It oscillates around its stable equilibrium
  - To settle at equilibrium, it must get rid of energy
  - Friction and air resistance help it settle

## Summary about Spring Scales

- The spring stretches during weighing
- This stretch is proportional to the weight
- The scale measures the spring's stretch
- The scale reports weight based on stretch

## Ball Sports: Bouncing

## Observations about Bouncing Balls

- Some balls bounce better than others
- Dropped balls don't rebound to their full height
- Balls bounce differently from different surfaces
- Ball bounce differently from moving objects

## 4 Questions about Bouncing Balls

- Why can't a ball that's dropped on a hard floor rebound to its starting height?
- Why does the floor's surface affect the bounce?
- How does a ball bounce when it hits a bat?
- What happens to the bat when a ball hits it?

## Question 1

- Why can't a ball that's dropped on a hard floor rebound to its starting height?
- What happens to ball's energy as it bounces?

## Bouncing from a Rigid Floor

- As it strikes a rigid floor, a ball's
  - kinetic energy decreases by the "collision" energy
  - elastic potential energy increases as it dents
- As it rebounds from that surface, the ball's
  - elastic potential energy decreases as it undents
  - kinetic energy increases by the "rebound" energy
- Rebound energy < collision energy
  - A "lively" ball wastes little energy as thermal energy
  - A "dead" ball wastes most of its energy

## Measuring a Ball's Liveliness

- Coefficient of Restitution
  - is a conventional measure of a ball's liveliness
  - is the ratio of outgoing to incoming speeds:

coefficient of restitution =  
outgoing speed / incoming speed

## Question 2

- Why does the floor's surface affect the bounce?



### Bouncing from an Elastic Floor

- Both ball and floor dent during a bounce
- Work is proportional to dent distance
- The denting floor stores and returns energy
  - A “lively” floor wastes little energy
  - A “dead” floor wastes most of its energy
- A floor has a coefficient of restitution, too
- A soft, lively floor can help the ball bounce!

### Question 3

- How does a ball bounce when it hits a bat?
- Do both the ball and bat bounce?

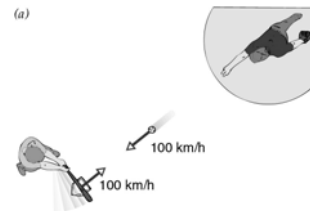
### Bouncing from Moving Surfaces

- Incoming speed → approaching speed
- Outgoing speed → separating speed
- Coefficient of Restitution becomes:

$$\text{coefficient of restitution} = \frac{\text{separating speed}}{\text{approaching speed}}$$

### Ball and Bat (Part 1)

- Ball heads toward home plate at 100 km/h
- Bat heads toward pitcher at 100 km/h
- Approaching speed is 200 km/h

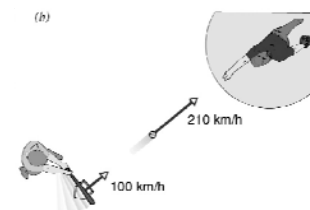


### Ball and Bat (Part 2)

- Approaching speed is 200 km/h
- Baseball’s coefficient of restitution: 0.55
- Separating speed is 110 km/h

### Ball and Bat (Part 3)

- Separating speed is 110 km/h
- Bat heads toward pitcher at 100 km/h
- Ball heads toward pitcher at 210 km/h



### Question 4

- What happens to the bat when a ball hits it?

### Bouncing's Effects on Objects

- A bouncing ball transfers momentum
  - while stopping
  - while rebounding
  - so a livelier ball transfers more momentum
- A bouncing ball can also transfer energy
- These two transfers together govern bouncing

### Impact Forces

- Harder surfaces bounce faster
  - Momentum is transferred more quickly
  - Time is shorter, so force is larger
- No one likes bouncing off hard surfaces

### The Ball's Effects on a Bat

- The ball pushes the bat back and twists it, too
- When the ball hits the bat's center of percussion,
  - the bat's backward and rotational motions balance
  - the bat's handle doesn't jerk
- When the ball hits the bat's vibrational node,
  - the bat doesn't vibrate
  - more energy goes into the ball

### Summary about Bouncing Balls

- Each ball has a coefficient of restitution
- Energy lost in a bounce becomes thermal
- The surface can affect a ball's bounce
- Surfaces bounce, too

### Carousels and Roller Coasters

### **Observations about Carousels and Roller Coasters**

- You can feel your motion with your eyes closed
- You feel pulled in unusual directions
- You sometimes feel weightless
- You can become inverted without feeling it

### **5 Questions about Carousels and Roller Coasters**

- What aspects of motion do you feel?
- Why do you feel flung outward on a carousel?
- Why do you feel light on a roller coaster's dives?
- Why do you feel heavy on a roller coaster's dips?
- How do you stay seated on a loop-the-loop?

### **Question 1**

- What aspects of motion do you feel?
  - Can you feel position?
  - Can you feel velocity?
  - Can you feel acceleration?

### **The Feeling of Weight**

- When you are at equilibrium,
  - a support force balances your weight
  - and that support force acts on your lower surface,
  - while your weight is spread throughout your body
- You feel internal supporting stresses
- You identify these stresses as weight

### **The Feeling of Acceleration**

- When you are accelerating,
  - a support force causes your acceleration
  - and that support force acts on your surface,
  - while your mass is spread throughout your body
- You feel internal supporting stresses
- You misidentify these stresses as weight

### **Acceleration and Weight**

- This "feeling of acceleration" is
  - not a real force
  - just a feeling caused by your body's inertia
  - directed opposite your acceleration
  - proportional to that acceleration
- You feel an overall "apparent weight"
  - feeling of real weight plus "feeling of acceleration"

## Question 2

- Why do you feel flung outward on a carousel?
- How are you accelerating on a carousel?

## Carousels (Part 1)

- Riders undergo “uniform circular motion”
  - They follow a circular path at constant speed
  - They are accelerating toward the circle’s center
  - This acceleration depends on speed and circle size  
 $\text{acceleration} = \text{velocity}^2 / \text{radius}$
- The acceleration of uniform circular motion is
  - a center-directed or centripetal acceleration
  - caused by a center-directed or centripetal force

## Carousels (Part 2)

- A centripetal acceleration
  - gives rise to a “feeling of acceleration”
  - that points away from the center of motion
  - and is an experience of inertia, not a real force
- This feeling is often called “centrifugal force”

## Questions 3 and 4

- Why do you feel light on a roller coaster’s dives?
- Why do you feel heavy on a roller coaster’s dips?

## Roller Coasters (Part 1 – Hills)

- During the dive down a hill,
  - acceleration is downhill
  - feeling of acceleration is uphill
  - apparent weight is weak and into the track
- During the dip at the bottom of a hill,
  - acceleration is approximately upward
  - feeling of acceleration is approximately downward
  - apparent weight is very strong and downward

## Question 5

- How do you stay seated on a loop-the-loop?

### **Roller Coasters (Part 2 – Loops)**

- At top of loop-the-loop,
  - acceleration is strongly downward
  - feeling of acceleration is strongly upward
  - apparent weight can point upward!

### **Choosing a Seat**

- As you go over cliff-shaped hills,
  - acceleration is downward
  - feeling of acceleration is upward
- The faster you dive over the first hill,
  - the greater the downward acceleration
  - the stronger the upward feeling of acceleration
- First car dives slowly – weak weightlessness
- Last car dives quickly – stronger weightlessness!

### **Summary about Carousels and Roller Coasters**

- You are often accelerating on these rides
- You experience feelings of acceleration
- Those feelings point opposite the acceleration
- Your apparent weight can
  - become larger or smaller than your real weight
  - point at any angle
  - can even point upward!

## **Bicycles**

### **Observations about Bicycles**

- They are hard to keep upright while stationary
- They stay upright easily while moving forward
- They require leaning during turns
- They can be ridden without hands

### **5 Questions about Bicycles**

- Why is a stationary tricycle so stable?
- Why is stationary bicycle so unstable?
- Why does a moving tricycle flip during turns?
- Why must you lean a bicycle during turns?
- Why can you ride a bicycle without hands?

### Question 1

- Why is a stationary tricycle so stable?

### Tricycles: Static Stability (Part 1)

- An upright tricycle has a “base of support”– the polygon formed by its ground contact points
- A tricycle has a center of gravity – the effective point at which its weight is located
- When center of gravity is above base of support, the tricycle is in a stable equilibrium:
  - Its gravitational potential starts to increase if it tips,
  - so it accelerates in the direction opposite the tip
  - and returns to the stable equilibrium.

### Tricycles: Static Stability (Part 2)

- When its center of gravity isn't above the base, the tricycle is not in equilibrium:
  - Its gravitational potential drops as it tips one way,
  - so it spontaneously accelerates in that direction
  - and it falls over.

### Tricycles: Static Stability (Part 3)

- When its center of gravity is above edge of base, the tricycle is in an unstable equilibrium:
  - Its gravitational potential starts decreasing if it tips,
  - so it accelerates in the direction of that tip
  - and doesn't return to the unstable equilibrium.

### Question 2

- Why is stationary bicycle so unstable?

### Bicycles: Static Instability

- A base of support requires 3 contact points
- An upright bicycle has only 2 contact points
  - An upright bicycle is in an unstable equilibrium
  - A stationary bicycle tips over easily

### Question 3

- Why does a moving tricycle flip during turns?

### Tricycles: Dynamic Instability

- When a tricycle is moving, inertia can take it in the direction opposite its acceleration and flip it,
  - so a stable equilibrium doesn't ensure stability.
- During a turn, the wheels accelerate to the inside
  - but the rider tends to coast straight ahead,
  - so the tricycle begins to tip.
  - The stabilizing acceleration appears but it's too slow
  - and the tricycle tips over anyway.
- Tricycle drives out from under center of gravity.

### Question 4

- Why must you lean a bicycle during turns?

### Bicycles: Dynamic Stability

- During a turn, the wheels accelerate to the inside
  - but a bicycle rider can lean to the inside of the turn
  - and therefore accelerate to the inside of the turn,
  - so the rider and bicycle turn together safely.
- The bicycle drives under center of gravity to return to the unstable equilibrium
- Motion can make a bicycle stable!

### Question 5

- Why can you ride a bicycle without hands?

### A Bicycle's Automatic Steering

- It naturally steers under its center of gravity
  - due to the design of its rotating front fork (the fork steers to reduce total potential energy)
  - due to gyroscopic precession of the front wheel (the ground's torque on spinning wheel steers it)
- A forward-moving bicycle that begins to tip
  - automatically returns to its unstable equilibrium,
  - and thus exhibits wonderful dynamic stability

## Summary about Bicycles

- Tricycles
  - have static stability
  - can flip during turns
- Bicycles
  - are statically unstable
  - can lean during turns to avoid flipping
  - automatically steer back to unstable equilibrium
  - have remarkable dynamic stability

## Rockets

### Observations about Rockets

- Plumes of flame emerge from rockets
- Rockets can accelerate straight up
- Rockets can go very fast
- The flame only touches the ground initially
- Rockets can apparently operate in empty space
- Rockets usually fly nose-first

### 6 Questions about Rockets

- What pushes a rocket forward?
- How does the rocket use its gas to obtain thrust?
- What keeps a rocket pointing forward?
- What limits a rocket's speed, if anything?
- Once in space, does a spaceship have a weight?
- What makes a spaceship orbit the earth?

### Question 1

- What pushes a rocket forward?

### Momentum Conservation

- A rocket's momentum is initially zero
- That momentum is redistributed during thrust
  - Ship pushes on fuel; fuel pushes on ship
  - Fuel acquires backward momentum
  - Ship acquires forward momentum
- Rocket's total momentum remains zero

$$\text{momentum}_{\text{fuel}} + \text{momentum}_{\text{ship}} = 0$$



## Rocket Propulsion

- The momenta of ship and fuel are opposite
- The ship's final momentum is

$$\begin{aligned} \text{momentum}_{\text{ship}} &= -\text{momentum}_{\text{fuel}} \\ &= -\text{mass}_{\text{fuel}} \cdot \text{velocity}_{\text{fuel}} \end{aligned}$$

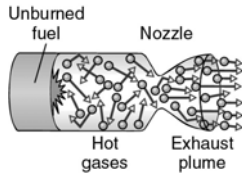
- The greater the fuel mass and backward velocity, the greater the ship's forward momentum

## Question 2

- How does the rocket use its gas to obtain thrust?

## Rocket Engines

- Combustion produces hot, high-pressure gas
- The gas speeds up in a de Laval nozzle
- Gas reaches sonic speed in the nozzle's throat
- Beyond the throat, supersonic gas expands to speed up further



## Question 3

- What keeps a rocket pointing forward?

## Stability and Orientation

- On the ground, a rocket needs static stability
- In the air, a rocket needs aerodynamic stability
  - Center of aerodynamic forces behind center of mass
- In space, a spaceship is a freely rotating object
  - Orientation governed by angular momentum
  - Small rockets are used to exert torques on spaceship
  - Spaceship's orientation doesn't affect its travel

## Question 4

- What limits a rocket's speed, if anything?

## Ship's Ultimate Speed

- Increases as
  - the ratio of fuel mass to ship mass increases
  - the fuel exhaust speed increases
- If fuel were released with the rocket at rest,

$$\text{velocity}_{\text{ship}} = -\frac{\text{mass}_{\text{fuel}} \cdot \text{velocity}_{\text{fuel}}}{\text{mass}_{\text{ship}}}$$

- But because rocket accelerates during thrust,

$$\text{velocity}_{\text{ship}} = -\log_e \left( \frac{\text{mass}_{\text{ship}} + \text{mass}_{\text{fuel}}}{\text{mass}_{\text{ship}}} \right) \cdot \text{velocity}_{\text{fuel}}$$

## Question 5

- Once in space, does a spaceship have a weight?

## Gravity (Part 1)

- The earth's acceleration due to gravity is only constant for small changes in height
- When the distance between two objects changes substantially, the relationship is:

$$\text{force} = \frac{\text{gravitational constant} \cdot \text{mass}_1 \cdot \text{mass}_2}{(\text{distance between masses})^2}$$

## Gravity (Part 2)

- The ship's weight is only constant for small changes in height
- When the ship's height changes significantly:

$$\text{weight} = \frac{\text{gravitational constant} \cdot \text{mass}_{\text{ship}} \cdot \text{mass}_{\text{earth}}}{(\text{distance between centers of ship and earth})^2}$$

## Gravity (Part 3)

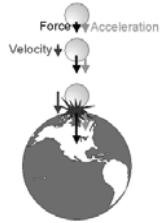
- Even far above earth, an object has weight
- Astronauts and spaceships have weights
  - weights are somewhat less than normal
  - weights depend on altitude
- Astronauts and spaceships are in free fall
  - Astronauts feel weightless because they are falling

## Question 6

- What makes a spaceship orbit the earth?

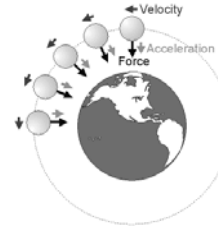
## Orbits (Part 1)

- An object that begins to fall from rest falls directly toward the earth
- Acceleration and velocity are in the same direction



## Orbits (Part 2)

- An object that has a sideways velocity follows a trajectory called an orbit
- Orbits can be closed or open, and are ellipses, parabolas, and hyperbolas



## Current Rocket Technology

- X-Prize Rockets
- Single State to Orbit Rockets
- Improbable Dreams
  - Rockets that rarely require refueling
  - Rockets that can land and leave large planets
  - Rockets that can turn on a dime in space

## Summary About Rockets

- Rockets are pushed forward by their fuel
- Total rocket impulse is basically the product of exhaust speed times exhaust mass
- Rockets can be stabilized aerodynamically
- Rockets can be stabilized by thrust alone
- After engine burn-out, spaceships can orbit

## Balloons

### Observations about Balloons

- Balloons are held taut by the gases inside
- Some balloons float in air while others don't
- Hot-air balloons don't have to be sealed
- Helium balloons "leak" even when sealed

## 5 Questions about Balloons

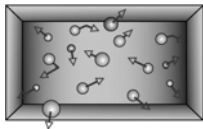
- How does air “inflate” a rubber balloon?
- Why doesn’t the atmosphere fall or collapse?
- Why does the atmosphere push up on a balloon?
- Why does a hot air balloon float in cold air?
- Why does a helium balloon float in air?

## Question 1

- How does air “inflate” a rubber balloon?
  - How does air occupy space?
  - How does air push on the balloon’s elastic skin?

## Air’s Characteristics

- Air is a gas
  - It consists of individual atoms and molecules
  - Its particles are kept separate by thermal energy
  - Its particles bounce around in free fall



## Air and Pressure

- Air has pressure
  - Air particles transfer momentum when they bounce
  - Each momentum transfer/bounce involves forces
  - Bouncing particles exerts forces on container walls
  - Average force is proportional to surface area
  - Average force per unit of area is called “pressure”



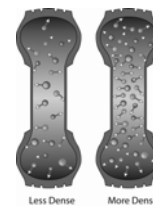
## Air and Density

- Air has density
  - Air particles have mass
  - Each volume of air has a mass
  - Average mass per unit of volume is called “density”



## Air Pressure and Density

- Air’s pressure is proportional to its density
  - In denser air, particles hit the surface more often
  - Denser air → more pressure



## Pressure Imbalances

- **Balanced pressure exerts no overall force**
  - Pressure forces on opposite sides of a balloon cancel
  - Sum of pressure forces on balloon is zero.
- **Unbalanced pressure exerts an overall force**
  - Forces on opposite sides of a balloon don't cancel
  - Sum of forces pushes balloon toward lower pressure
- **Unbalanced pressure affects the air itself**
  - The air is pushed toward lower pressure

## Question 2

- **Why doesn't the atmosphere fall or collapse?**
  - Air has weight, so why doesn't it fall to the ground?
  - How is the atmosphere supported against gravity?
  - Why is the air denser at lower altitudes?

## The Atmosphere

- **The atmosphere is in stable equilibrium**
  - Air pressure decreases with altitude
  - A pressure imbalance pushes each air layer upward
  - This upward force balances the layer's weight
  - Air near the ground supports the air overhead
- **Supporting itself structures the atmosphere**
  - Air pressure is highest near the ground
  - Air density is highest near the ground

## Question 3

- **Why does the atmosphere push up on a balloon?**

## The Buoyant Force

- **Because of atmospheric structure, air pressure is**
  - stronger near the bottom of a balloon,
  - weaker near the top of the balloon,
  - so the air pushes up harder than it pushes down,
  - and this imbalance yields an upward buoyant force
- **The atmosphere pushes upward on the balloon!**

## Archimedes' Principle

- **A balloon immersed in a fluid experience an upward buoyant force equal to the weight of the fluid it displaces**

### Question 4

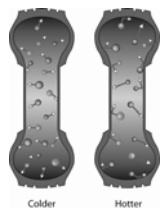
- Why does a hot air balloon float in cold air?
  - Why does a cold air balloon sink in cold air?
  - What is the difference between hot air and cold air?

### Room-Air Balloon in Air

- A rubber balloon filled with room air
  - weighs more than the room air it displaces,
  - experiences a downward net force in room air,
  - and sinks in room air
- Balloon's average density  $>$  room air's density

### Air and Temperature

- Air pressure is proportional to temperature
  - Faster particles hit surface harder and more often
  - Hotter air  $\rightarrow$  more pressure



### An Aside About Temperature

- Like most things, air has a temperature
  - Air particles have thermal kinetic energy
  - Average thermal kinetic energy per particle is proportional to absolute temperature
- SI unit of absolute temperature: kelvins or K
  - 0 K is absolute zero: no thermal energy left
  - Step size: 1 K step same as 1 °C step
  - Room temperature is approximately 300 K

### Hot-Air Balloon in Air

- A rubber balloon filled with hot air
  - contains fewer air particles than if it were cold,
  - weighs less than the room air it displaces,
  - experiences an upward net force in room air,
  - and floats in room air
- Balloon's average density  $<$  room air's density

### Question 5

- Why does a helium balloon float in air?
  - How does helium differ from air?
  - Doesn't helium have mass and weight?

### **Pressure and Particle Density**

- A volume of gas has some number of particles
- The average number of gas particles per unit of volume is called the gas's "particle density"
- All gas particles contribute equally to pressure
  - lower-mass particles travel faster and bounce more,
  - so all the effects of particle mass cancel out
- Gases with equal particle densities and equal temperatures have equal pressures

### **Helium vs. Air**

- A helium atom has less mass than an air particle
- At the same temperature, a helium balloon has
  - the same pressure as an air balloon,
  - the same particle density as an air balloon,
  - and therefore less mass than an air balloon

### **Helium Balloon in Air**

- A rubber balloon filled with helium
  - has same particle density as air,
  - weighs less than the air it displaces,
  - experiences an upward net force in air,
  - and floats in air
- Balloon's average density < room air's density

### **The Ideal Gas Law**

- is a summary relationship for gases:  
pressure = Boltzmann constant · particle density · absolute temperature
- and it assumes perfectly independent particles
  - While real gas particles aren't perfectly independent,
  - this law is still a good approximation for real gases

### **Summary about Balloons**

- A balloon will float if its average density is less than that of the surrounding air
- A hot-air balloon has a lower particle density and a lower density than the surrounding air
- A helium balloon has the same particle density but a lower density than the surrounding air

### **Water Distribution**

## Observations about Water Distribution

- Water is pressurized in the pipes
- Higher pressure water can spray harder
- Higher pressure water can spray higher
- Water is often stored high up in water towers

## 4 Questions about Water Distr.

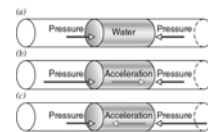
- Why does water move through level pipes?
- How can you produce pressurized water?
- Where does the work you do pumping water go?
- As water flows, what happens to its energy?

## Question 1

- Why does water move through level pipes?
  - Can water in a level pipe move without a push?
  - How does water in a level pipe respond to a push?
  - How do you push on water in a level pipe?

## How Water Moves (no gravity)

- Water, like all fluids, obeys Newton's laws
  - When water experiences zero net force, it coasts
  - When water experiences a net force, it accelerates
  - Pressure imbalances exert net forces on water
  - Water accelerates toward lower pressure



## Question 2

- How can you produce pressurized water?
  - How can you create pressure?
  - How can you deliver pressurized water to a pipe?
  - Why does pumping water require such effort?

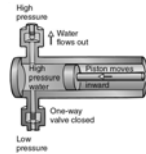
## Pressurizing Water

- To pressurize water, confine it and squeeze
  - As you push inward on the water,
  - it pushes outward on you (Newton's third law).
  - Water's outward push is produced by its pressure,
  - so the water's pressure rises as you squeeze it harder.



### **Pumping Water (no gravity)**

- To deliver pressurized water to a pipe,
  - squeeze water to increase its pressure
  - until that pressure exceeds the pressure in the pipe.
  - The water will then accelerate toward the pipe
  - and pressurized water will flow into the pipe!



### **Pumping Requires Work**

- You do work as you pump water into the pipe
  - You squeeze the water inward – the force,
  - and the water moves inward – the distance.
  - In this case, the work you do is:  
$$\text{work} = \text{pressure} \cdot \text{volume}$$
- The pressurized water carries your work with it
- We'll call this work “pressure potential energy”

### **Question 3**

- Where does the work you do pumping water go?

### **Pressure Potential Energy**

- Pressure potential energy is unusual because
  - it's not really stored in the pressurized water,
  - it's promised by the water's pressure source.
- In steady state flow (SSF),
  - which is steady flow in motionless surroundings,
  - promised energy is as good as stored energy
  - so pressure potential energy (PPE) is meaningful.

### **Question 4**

- As water flows, what happens to its energy?

### **Energy and Bernoulli (no gravity)**

- In SSF, water flows along streamlines
- Water flowing along a single streamline in SSF
  - has both PPE and kinetic energy (KE),
  - must have a constant total energy per volume,
  - and obeys Bernoulli's equation (no gravity):  
$$\text{PPE}/\text{Vol} + \text{KE}/\text{Vol} = \text{Constant}/\text{Vol}$$

### **How Water Moves (with gravity)**

- Weight contributes to the net force on water
- Without a pressure imbalance, water falls
- Water in equilibrium has a pressure gradient
  - Its pressure decreases with altitude
  - Its pressure increases with depth
- Water has gravitational potential energy (GPE)

### **Energy and Bernoulli (with gravity)**

- Water flowing along a single streamline in SSF
  - has PPE, KE, and GPE,
  - must have a constant total energy per volume,
  - and obeys Bernoulli's equation (with gravity):
$$\text{PPE/Vol} + \text{KE/Vol} + \text{GPE/Vol} = \text{Constant/Vol}$$

### **Energy Transformations (part 1)**

- As water flows upward in a uniform pipe,
  - its speed can't change (a jam or a gap would form),
  - so its gravitational potential energy increases
  - and its pressure potential energy decreases.
- As water flows downward in a uniform pipe,
  - its speed can't change,
  - so its gravitational potential energy decreases
  - and its pressure potential energy increases.

### **Energy Transformations (part 2)**

- As water rises upward from a fountain nozzle,
  - its pressure stays constant (atmospheric),
  - so its gravitational potential energy increases
  - and its kinetic energy decreases.
- As water falls downward from a spout,
  - its pressure stays constant (atmospheric),
  - so its gravitational potential energy decreases
  - and its kinetic energy increases.

### **Energy Transformations (part 3)**

- As water sprays horizontally from a nozzle,
  - its height is constant,
  - so its kinetic energy increases
  - and its pressure potential energy decreases.
- As a horizontal stream of water hits a wall,
  - its height is constant,
  - so its kinetic energy decreases
  - and its pressure potential energy increases.

### **Summary about Water Distribution**

- Water's energy remains constant during SSF
- Water's energy changes form as it
  - flows upward or downward inside pipes,
  - rises or falls in open sprays,
  - and shoots out of nozzles or collides with objects.
- Water distribution can driven by
  - pressurized water (PPE)
  - elevated water (GPE)
  - fast-moving water (KE)

## Garden Watering

### Observations about Garden Watering

- Faucets allow you to control water flow
- Faucets make noise when open
- Longer, thinner hoses deliver less water
- Water sprays faster from a nozzle
- Water only sprays so high
- A jet of water can push things over

### 6 Questions about Garden Watering

- How does a faucet control flow?
- How much does the diameter of a hose matter?
- Why does water pour gently from an open hose?
- Why does water spray so hard from a nozzle?
- What causes hissing in a faucet, hose, or nozzle?
- Why do pipes rattle when you close the faucet?

### Question 1

- How does a faucet control flow?
  - Why is a small opening different from a large one?

### Faucets and Water Flow

- In going through a faucet, water must
  - flow through a narrow passage
  - and pass close to the faucet's stationary surfaces
- Total energy limits flow speed through passage
  - The water turns its total energy into kinetic energy,
  - but its peak speed is limited by its initial pressure
- Motion near the surfaces slows the water
  - Because water at the walls is stationary,
  - viscous forces within the water slow all of it

### Viscous Forces and Viscosity

- Viscous forces
  - oppose relative motion within a fluid
  - and are similar to sliding friction: they waste energy
- Fluids are characterized by their viscosities
  - the measure of the strength of the viscous forces
  - and caused by chemical interactions with the fluids

## Question 2

- How much does the diameter of a hose matter?
  - Is a 5/8" hose much different from a 3/4" hose?

## Hoses and Water Flow (part 1)

- The rate at which water flows through a hose,
  - increases as end-to-end pressure difference increases,
  - decreases as water's viscosity increases,
  - decreases as the hose becomes longer,
  - and increases *dramatically* as the hose becomes wider
- Increasing the hose width
  - enlarges cross-sectional area through which to flow
  - and lets water get farther from the walls of the hose

## Hoses and Water Flow (part 2)

- Water flow through a hose is proportional to
  - pressure difference
  - 1/viscosity
  - 1/hose length
  - (pipe diameter)<sup>4</sup>
- Poiseuille's law:

$$\text{flow rate} = \frac{\pi \cdot \text{pressure difference} \cdot \text{pipe diameter}^4}{128 \cdot \text{pipe length} \cdot \text{viscosity}}$$

## Question 3

- Why does water pour gently from an open hose?

## Wasting Energy in a Hose

- Viscous effects
  - waste water's total energy as thermal energy
  - and become stronger with increased flow speed
- Faster flow leads to more viscous energy loss
- Faster flow causes quicker loss of pressure

## Question 4

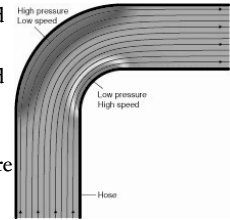
- Why does water spray so hard from a nozzle?

## Making Water Accelerate

- Even in steady-state, water can accelerate
  - but forward acceleration would leave gaps
  - and backward acceleration would cause jams,
  - so the acceleration must involve turning
- Acceleration toward the side (turning)
  - requires obstacles,
  - and involves pressure imbalances
  - and changes in speed

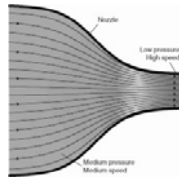
## Bending the Flow in a Hose

- Since water accelerates toward lower pressure,
- water flow needs a pressure imbalance to bend
- The flow naturally develops a pressure gradient
  - higher pressure & lower speed on the outside of the bend
  - lower pressure & higher speed on the inside of the bend
  - and water accelerates from high pressure to lower pressure



## Speeding the Flow in a Nozzle

- Since water must speed up through a nozzle,
- it needs a pressure imbalance to push it forward
- The flow naturally develops a pressure gradient
  - lower pressure & higher speed as the neck narrows



## Question 5

- What causes hissing in a faucet, hose, or nozzle?

## Water Flow Isn't Always Smooth

- We've been examining laminar flow
  - in which viscosity dominates the flow's behavior
  - and nearby regions of water remain nearby
- Now we'll also consider turbulent flow
  - in which inertia dominates the flow's behavior
  - and nearby regions of water become separated

## Reynolds Number

- The flow type depends on the Reynolds number

$$\text{Reynolds number} = \frac{\text{inertial influences}}{\text{viscous influences}} = \frac{\text{density} \cdot \text{obstacle length} \cdot \text{flow speed}}{\text{viscosity}}$$

- Below ~2300 viscosity wins, so flow is laminar
- Above ~2300 inertia wins, so flow is turbulent

### Question 6

- Why do pipes rattle when you close the faucet?

### Water and Momentum

- Water carries momentum
- Water transfers its momentum via impulses:  
impulse = pressure · surface area · time
- Large momentum transfers requires
  - large pressures,
  - large surface areas,
  - and/or long times.
- Moving water can be surprisingly hard to stop

### Summary about Garden Watering

- Total energy limits speed, height, and pressure
- Bending water flows develop pressure gradients
- Nozzles exchange pressure for speed
- Viscosity wastes flowing water's total energy
- Turbulence wastes flowing water's total energy
- Wasted total energy because thermal energy
- Moving water has momentum, too

### Balls and Air

### Observations about Balls and Air

- Air resistance slows a ball down
- The faster a ball moves, the quicker it slows
- Some balls have deliberately roughened surfaces
- Spinning balls curve in flight

### 3 Questions about Balls and Air

- Why do balls experience air resistance?
- Why do some balls have dimples?
- Why do spinning balls curve in flight?

## Question 1

- Why do balls experience air resistance?
  - Do viscous forces slow balls?
  - Does air pressure slow balls?

## Aerodynamic Forces: Drag

- Air resistance is technically called “drag”
- When a ball moves through air, drag forces arise
  - The air pushes the ball downstream
  - and the ball pushes the air upstream
- Drag forces transfer momentum
  - air transfers downstream momentum to ball
  - ball transfers upstream momentum to air

## Aerodynamic Forces: Lift

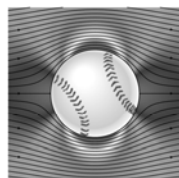
- When a ball deflects passing air, lift forces arise
  - The air pushes the ball to one side
  - and the ball pushes the air to the other side
- Lift forces transfer momentum
  - air transfers sideways momentum to ball
  - ball transfers sideways momentum to air
- Lift forces don't always point upward!

## Types of Drag & Lift

- Surface friction causes viscous drag
- Turbulence causes pressure drag
- Deflected flow causes lift
- Deflected flow also leads to induced drag

## Perfect Flow Around a Ball

- Air bends away from ball's front
  - At front: high pressure, slow flow
- Air bends toward ball's sides
  - At side: low pressure, fast flow
- Air bends away from ball's back
  - At back: high pressure, slow flow
- Pressures on opposite sides balance perfectly,
- so ball experiences only viscous drag.

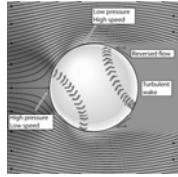


## The Onset of Turbulence

- Air flowing into the rising pressure behind ball
  - accelerates backward (decelerates)
  - and converts kinetic energy into pressure potential.
- Air flowing nearest the ball's surface
  - also experiences viscous drag
  - and converts kinetic energy into thermal energy.
  - If it runs out of total energy, it stops or “stalls”
- If air nearest the ball stalls, turbulence ensues

## Imperfect Flow Around Slow Ball

- Air flowing near ball's surface
  - stalls beyond ball's sides
  - and peels main air flow off of ball.
- Big wake forms behind ball
  - Since wake pressure is ambient,
  - ball experiences unbalanced pressures.
- Ball experiences a large pressure drag force



## Question 2

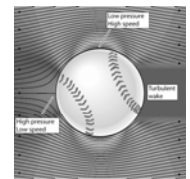
- Why do some balls have dimples?

## Boundary Layer

- Flow near the surface forms a "boundary layer"
- At low Reynolds number ( $<100,000$ )
  - the boundary layer is laminar,
  - so closest layer is slowed relentlessly by viscous drag
- At high Reynolds number ( $>100,000$ )
  - the boundary layer itself is turbulent,
  - so tumbling continually renews closest layer's energy
  - boundary layer penetrates deeper into rising pressure

## Imperfect Flow Around Fast Ball

- Air flowing near ball's surface
  - stalls beyond ball's sides
  - and peels main air flow off of ball.
- Boundary layer is turbulent
  - and retains total energy farther,
  - so it resists peeling better.
- Small wake forms behind ball
- Ball experiences a small pressure drag force



## Tripping the Boundary Layer

- To reduce pressure drag, some balls have dimples
  - Dimples "trip" the boundary layer
  - and causes boundary layer to become turbulent.
  - Since turbulent boundary layer resists peeling better,
  - ball's main airflow forms smaller turbulent wake.
- Example: Golf balls

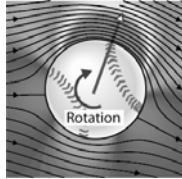
## Question 3

- Why do spinning balls curve in flight?



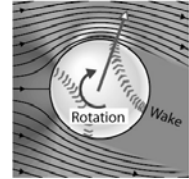
### Spinning Balls, Magnus Force

- Turning surface pushes/pulls on the air flow
  - Air on one side makes long bend toward ball
  - Air on other side makes shorter bend away from ball
  - Pressures are unbalanced
- The overall air flow is deflected
  - Ball pushes air to one side
  - Air pushes ball to other side
- Ball feels Magnus lift force



### Spinning Balls, Wake Force

- Turning surface alters point of flow separation
  - Flow separation is delayed on one side
  - and hastened on the other side,
  - so wake is asymmetric
- The overall air flow is deflected
  - Ball pushes air to one side
  - Air pushes ball to other side
- Ball feels Wake lift force



### Summary about Balls and Air

- The air pressures around these objects are not uniform and result in drag and lift
- Balls experience mostly pressure drag
- Spinning balls experience Magnus and Wake Deflection lift forces

## Airplanes

### Observations about Airplanes

- Airplanes use the air to support themselves
- Airplanes need airspeed to stay aloft
- Airplanes seem to follow their nose, up or down
- Airplanes can rise only so quickly
- Airplane wings often change shape in flight
- Airplanes have various propulsion systems

### 6 Questions about Airplanes

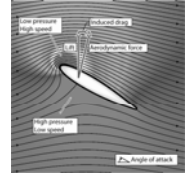
- How does an airplane support itself in the air?
- How does the airplane “lift off” the runway?
- Why does plane tilt up to rise; down to descend?
- Why are there different wing shapes?
- How does a plane turn?
- How does a plane propel itself through the air?

## Question 1

- How does an airplane support itself in the air?
  - What pushes up on airplane to balance its weight?
  - What does it do with the momentum gravity gives it?

## Using a Wing to Obtain Lift (part 1)

- As air flows under a wing,
  - air bends away from the wing
  - air's pressure rises, speed drops
- As air flows over the wing,
  - air bends toward the wing
  - air's pressure drops, speed rises
- The wing experiences a pressure imbalance
- There is an upward pressure force on the wing



## Using a Wing to Obtain Lift (part 2)

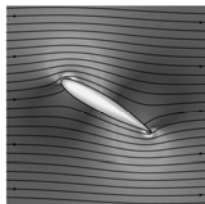
- The wing experiences
  - a strong upward lift force
  - a small downstream drag force
- Wing pushes air down, air pushes wing up!
- Downward momentum is transferred
  - from the earth to the airplane by gravity,
  - from the airplane to the air by lift forces, and
  - from the air to the earth by pressure on the ground

## Question 2

- How does the airplane "lift off" the runway?
  - How does the pilot initiate the rise?
  - How is landing different from takeoff?

## At Take-Off

- As a wing starts moving in air
  - the airflow is symmetric
  - and the wing experiences no lift
- However, this airflow is
  - unstable at trailing edge kink
  - and the wing sheds a vortex
- After the vortex leaves, the wing has lift



## Question 3

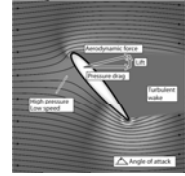
- Why does plane tilt up to rise; down to descend?
  - Does a plane always go in the direction it's pointed?
  - How can plane land if its nose is higher than its tail?

## Angle of Attack

- A wing's lift depends on
  - the shape of its airfoil
  - and on its angle of attack—its tilt relative to the wind
- Tilting an airplane's wings
  - changes the net force on the airplane
  - and can make the airplane accelerate up or down
  - but usually requires tilting the airplane's fuselage
- Plane's tilt controls lift, not direction of travel

## Limits to Lift: Stalling

- At too great an angle of attack,
  - the upper boundary layer stalls,
  - the airstream detaches from wing,
  - the lift nearly vanishes,
  - and pressure drag appears
- Plane plummets abruptly

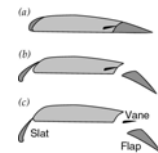


## Question 4

- Why are there different wing shapes?

## Wing Shape

- Asymmetric airfoils produce large lifts
  - They are well suited to low-speed flight
- Symmetric airfoils produce small lifts
  - They are well suited to high-speed flight
  - and allow plane to fly inverted easily
- High-speed planes often change wing shape in flight



## Question 5

- How does a plane turn?

## Turning and Orientation

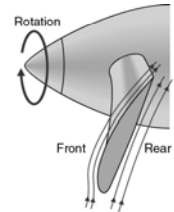
- Airplanes also use lift to accelerate to the side
- Three orientation controls:
  - Angle of attack controlled by elevators
  - Left-right tilt controlled by ailerons
  - Left-right rotation controlled by rudder
- Steering involves ailerons and rudder
- Elevation involves elevators and engine

## Question 6

- How does a plane propel itself through the air?
  - How does a plane maintain its forward momentum?

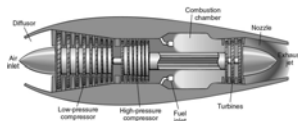
## Propellers

- Propellers are spinning wings
  - They deflect air backward,
  - do work on air (add energy),
  - and pump air toward rear of plane
- Action-Reaction
  - They push the air backward,
  - so air pushes them forward



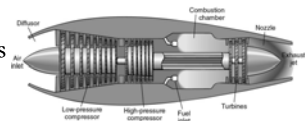
## Jet Engines (Part 1)

- Jet engines pump air toward rear of plane
  - Engine consists of an oval “ball” with a complicated duct or passageway through it
  - Air passing through the duct exchanges first speed for pressure and then pressure for speed
  - Engine adds energy to air inside the duct



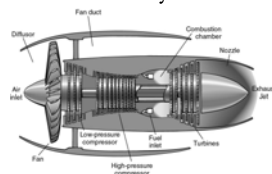
## Jet Engines (Part 2)

- Air entering diffuser slows and its pressure rises
- Compressor does work on air
- Fuel is added to air and that mixture is burned
- Expanding exhaust gas does work on turbine
- As exhaust leaves nozzle it speeds up and its pressure drops



## Jet Engines (Part 3)

- Turbojet obtains forward momentum by
  - moving relatively little air
  - and giving that air too much energy
- Turbofan obtains forward momentum by
  - moving much more air
  - giving that air less energy



## Summary about Airplanes

- Airplanes use lift to support themselves
- Propulsion overcomes induced drag
- Speed and angle of attack affect altitude
- Extreme angle of attack causes stalling
- Propellers do work on passing airstream
- Jet engines do work on slowed airstream

## Woodstoves

### Observations about Woodstoves

- They burn wood in enclosed fireboxes
- They often have long chimney pipes
- Their surfaces are usually darkly coated
- They'll burn you if you touch them
- Heat rises off their surfaces
- They warm you when you stand near them

### 5 Questions about Wood Stoves

- What are thermal energy and heat?
- How does a woodstove produce thermal energy?
- Why does heat flow from the stove to the room?
- Why is a woodstove better than an open fire?
- How does a woodstove heat the room?

### Question 1

- What are thermal energy and heat?
  - What is the difference between those two quantities?
  - Can those terms be used interchangeably?

### Having Thermal Energy

- Thermal energy is
  - disordered energy within an object,
  - the kinetic and potential energies of its atoms,
  - and is responsible for temperature
- Thermal energy doesn't include order energies:
  - kinetic energy of an object moving or rotating
  - potential energy of outside interactions

### Transferring Heat

- Heat is
  - energy that flows between objects because of their difference in temperature.
  - thermal energy on the move.
- Technically, objects don't contain "heat"

## Question 2

- How does a woodstove produce thermal energy?

## Burning Wood

- Fire releases chemical potential energy
  - Wood and air consist of molecules
  - Molecules are bound by chemical bonds
  - When bonds rearrange, they can release energy
  - Burning rearranges bonds and releases energy!

## Chemical Forces and Bonds

- Atoms interact via electromagnetic forces
- The chemical forces between two atoms are
  - attractive at long distances,
  - repulsive at short distances,
  - and zero at a specific equilibrium separation
- Atoms at the equilibrium separation
  - are in a stable equilibrium
  - and are bound together by an energy deficit

## A Few Names

- Molecule: atoms joined by chemical bonds
- Chemical bond: a chemical-force linkage
- Bond strength: the work needed to break bond
- Reactants: starting molecules
- Products: ending molecules

## Chemical Reactions

- Breaking old bonds takes work
- Forming new bonds does work
- If new bonds are stronger than the old bonds,
  - chemical potential energy  $\rightarrow$  thermal energy
- Breaking old bonds requires energy
  - reaction requires activation energy to start

## When Wood Burns...

- When you ignite wood,
  - the reactants are carbohydrates and oxygen
  - the products are water and carbon dioxide
  - the activation energy comes from a burning match
- This reaction releases energy as thermal energy

### Question 3

- Why does heat flow from the stove to the room?

### Heat and Temperature

- Heat always flows from hotter to colder
  - Microscopically, thermal energy moves both ways
  - But statistically, the net flow is from hotter to colder
- At thermal equilibrium
  - the temperatures of the objects are equal
  - and no heat flows between those objects
- Temperature is (approximately) the average thermal kinetic energy per particle

### Question 4

- Why is a woodstove better than an open fire?

### An Open Fire

- Burns wood to release thermal energy
- It has good features:
  - Heat flows from hot fire to cold room
- But it also has bad features:
  - Smoke enters room
  - Fire uses up room's oxygen
  - Can set fire to room

### A Fireplace

- Burns wood to release thermal energy
- It has good features:
  - Heat flows from hot fire to cold room
  - Smoke goes mostly up chimney
  - New oxygen enters room through cracks
  - Less likely to set fire on room
- And it has bad features:
  - Inefficient at transferring heat to room

### A Woodstove

- Burns wood to release thermal energy
- It has good features:
  - Heat flows from hot fire to cold room
  - All the smoke goes up chimney pipe
  - New oxygen enters room through cracks or vents
  - Relatively little fire hazard
  - Transfers heat efficiently to room

## Heat Exchangers

- Woodstove is a heat exchanger
  - Separates air used by the fire from room air
  - Transfers heat without transferring smoke

## Question 5

- How does a woodstove heat the room?

## Heat Transfer Mechanisms

- Conduction: heat flow through materials
- Convection: heat flow via moving fluids
- Radiation: heat flow via light waves
- All three transfer heat from hot to cold

## Conduction and Woodstoves

- Heat flows but atoms don't
- In an insulator,
  - adjacent atoms jiggle one another
  - atoms do work and exchange energies
  - on average, heat flows from hot to cold atoms
- In a conductor,
  - mobile electrons carry heat long distances
  - heat flows quickly from hot to cold spots
- Conduction moves heat through stove's walls

## Convection and Woodstoves

- Fluid transports heat stored in its atoms
  - Fluid warms up near a hot object
  - Flowing fluid carries thermal energy with it
  - Fluid cools down near a cold object
  - Overall, heat flows from hot to cold
- Natural buoyancy drives convection
  - Warmed fluid rises away from hot object
  - Cooled fluid descends away from cold object
- Convection circulates hot air around the room

## Radiation and Woodstoves

- Heat flows by electromagnetic waves (radio waves, microwaves, light, ...)
- Wave types depend on temperature
  - cold: radio wave, microwaves, infrared light
  - hot: infrared, visible, and ultraviolet light
- Higher temperature → more radiated heat
- Black emits and absorbs light best



## Stefan-Boltzmann Law

- The amount of heat a surface radiates is

$$\text{power} = \text{emissivity} \cdot \text{Stefan-Boltzmann constant} \cdot \text{temperature}^4 \cdot \text{surface area}$$

- where emissivity is the measure of emission efficiency
- Emissivity
  - 0 is perfect inefficiency: white, shiny, or clear
  - 1 is perfect efficiency: black
- Radiation transfers heat to your skin as light

## What About Campfires?

- No conduction, unless you touch hot coals
- No convection, unless you are above fire
- Lots of radiation:
  - your face feels hot because radiation reaches it
  - your back feels cold because no radiation reaches it

## Summary about Wood Stoves

- Use all three heat transfer mechanisms
- Have tall chimneys for heat exchange
- Are dark-coated to encourage radiation
- Are sealed to keep smoke out of room air

## Water, Steam, and Ice

### Observations about Water, Steam, and Ice

- Water has three forms or phases
- Ice is typically present below 32 °F (0 °C)
- Water is typically present above 32 °F (0 °C)
- Steam is typically present at high temps
- The three phases sometimes coexist

### 4 Questions about Water, Steam, Ice

- How can water and ice coexist in a glass?
- Can steam exist below 212 °F (100 °C)?
- Where do ice cubes go in a frostless freezer?
- Is salt the only chemical that helps melt ice?

### Question 1

- How can water and ice coexist in a glass?

### Phases of Matter

- Ice is solid: fixed volume and fixed shape
- Water is liquid: fixed volume but variable shape
- Steam is gas: variable volume and variable shape

### Phase Equilibrium

- When two (or more) phases are present
  - molecules continually shift between the phases
  - one phase may grow at the expense of another phase
  - that growth often requires or releases thermal energy
- At phase equilibrium,
  - two (or more) phases can coexist indefinitely
  - neither phase grows at the expense of the other

### Ice and Water

- Ice has a melting temperature 32 °F (0 °C)
  - below which solid ice is the stable phase,
  - above which liquid water is the stable phase,
  - and at which ice and water can coexist
- To melt ice at 32 °F (0 °C),
  - destabilize ice relative to water by
    - adding heat
    - or increasing pressure (very atypical!)

### Ice and Water (con't)

- To freeze water at 32 °F (0 °C),
  - destabilize water relative to ice by
    - removing heat
    - or decrease pressure (very atypical!)
- Melting ice requires the latent heat of melting

### Question 2

- Can steam exist below 212 °F (100 °C)?

## Water and Steam

- Liquid water and gaseous steam
  - can coexist over a broad range of temperatures
  - but equilibrium steam density rises with temperature
- To evaporate water,
  - destabilize water relative to steam by
    - adding heat
    - or reducing steam density

## Water and Steam (con't)

- To condense steam,
  - destabilize steam relative to water
  - removing heat
  - or increasing steam density
- Evaporating water requires latent heat of evaporation

## Boiling (Part 1)

- Evaporation bubbles can form inside water
  - Pressure in steam bubble depends on steam density
  - When steam pressure exceeds ambient pressure, steam bubble survives and grows
- Boiling occurs when
  - bubbles can nucleate (when seed bubbles form)
  - bubbles can grow via evaporation
- Need for latent heat stabilizes temperature

## Boiling (Part 2)

- Boiling temperature depends on ambient pressure
  - Elevated pressure raises boiling temperature
  - Diminished pressure lowers boiling temperature
- Cooking uses boiling to set a stable temperature
  - Foods cook fast at high pressures (sea level)
  - Foods cook slow at low pressures (high altitudes)

## Question 3

- Where do ice cubes go in a frostless freezer?

## Ice and Steam

- Solid ice and gaseous steam
  - can coexist over a broad range of temperatures
  - but equilibrium steam density rises with temperature
- To sublime ice,
  - destabilize ice relative to steam by
    - adding heat
    - or reducing steam density

### Ice and Steam (con't)

- To deposit steam,
  - destabilize steam relative to ice by
    - removing heat
    - or increasing steam density
- Subliming ice requires latent heats of melting *and* evaporation

### Relative Humidity

- At 100% relative humidity,
  - ( $< 0\text{ }^{\circ}\text{C}$ ) ice is in phase equilibrium with steam
  - ( $> 0\text{ }^{\circ}\text{C}$ ) water is in phase equilibrium with steam
- Below 100% relative humidity,
  - ( $< 0\text{ }^{\circ}\text{C}$ ) ice sublimates (goodbye ice cubes!)
  - ( $> 0\text{ }^{\circ}\text{C}$ ) water evaporates
- Above 100% relative humidity,
  - ( $< 0\text{ }^{\circ}\text{C}$ ) frost forms
  - ( $> 0\text{ }^{\circ}\text{C}$ ) steam condenses

### Question 4

- Is salt the only chemical that helps melt ice?

### Effects of Impurities

- Dissolved impurities stabilize liquid water,
  - so its melting temperature drops
  - and its boiling temperature rises
- These shifts are proportional to solute density,
  - such as the density of salt ions in the water
  - or the density of sugar molecules
- Any soluble material can help ice to melt
- Insoluble materials don't cause ice to melt

### Summary about Water, Steam, and Ice

- Phase transitions reflect relative phase stabilities
- Phases in equilibrium are equally stable
- Temperature and pressure affect phase stabilities
- Phase transitions usually require or release heat

### Clothing, Insulation, and Climate

## Observations about Clothing, Insulation, and Climate

- Clothing keeps you warm in cold places
- Clothing can keep you cool in very hot places
- Insulation controls heat flow in various objects
- Insulation can be obvious, as in foam cups
- Insulation can be subtle, as in special windows
- Greenhouse gases trap heat and warm the earth

## 4 Questions about Clothing, Insulation, and Climate

- How does clothing control thermal conduction?
- How does clothing control thermal convection?
- How does insulation control thermal radiation?
- Why do greenhouse gases warm the earth?

### Question 1

- How does clothing control thermal conduction?

### Thermal Conductivity

- Heat naturally flows from hot to cold
- If one end of a material is hotter than the other
  - it will conduct heat from its hot end to its cold end
  - at a rate equal to the material's area,
  - times the temperature difference,
  - times the material's thermal conductivity,
  - divided by the material's thickness.

$$\text{heat flow} = \frac{\text{thermal conductivity} \cdot \text{temperature difference} \cdot \text{area}}{\text{thickness}}$$

### Limiting Thermal Conduction

- Clothing is often intended to reduce heat flow
  - so it should use low-thermal conductivity materials
    - electrical insulators, not metals
    - materials that trap air—air is a very poor thermal conductor
  - and it should use relatively thick materials
    - wool sweaters, down coats, heavy blankets
- Reducing exposed area is helpful when possible
- Reducing the temperature difference always helps

### Question 2

- How does clothing control thermal convection?

## Natural Convection

- Heat naturally flows from hot to cold
- If one region of a fluid is hotter than the other
  - those regions will also have different densities
  - and buoyancy may cause the fluid to circulate.
- The rate of heat flow depends on
  - the heat capacity and mobility of the fluid
  - how quickly heat flows into or out of the fluid
  - how well buoyancy circulates fluid from hot to cold

## Forced Convection

- Buoyancy isn't always effective at moving fluids
  - It fails when the hotter fluid is above the colder fluid
  - It fails when fluids experience large drag forces
  - It fails in certain awkward geometries
- Stirring the fluid enhances heat flow
  - Wind leads to faster heat transfer (wind chill)
  - Moving through air or water speeds heat transfer

## Limiting Thermal Convection

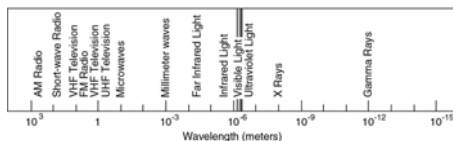
- Clothing can reduce convective heat flow by
  - preventing fluids from circulating
  - reducing temperature differences in the fluid
- The most effective clothing is thick and fluffy
  - The fluffiness traps air so that it can't convect
  - The thickness allows the surface temperature to drop to that of your surroundings so that there is no external convection
- A wind breaker minimizes forced convection

## Question 3

- How does insulation control thermal radiation?

## Thermal Radiation

- Materials all emit thermal radiation because
  - they contain electric charges
  - and thermal energy causes those charges accelerate.
  - Accelerating charges emit electromagnetic waves
- Hotter temperatures yield shorter wavelengths

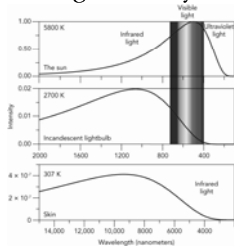


## Black Body Spectrum (Part 1)

- A surface's efficiency at absorbing and emitting thermal radiation is measured by its emissivity
  - 1 for a perfect emitter-absorber (black)
  - 0 for a nonemitter-nonabsorber (white, clear, shiny)
- The spectrum and intensity of a black surface's thermal radiation depend only on its temperature

## Black Body Spectrum (Part 2)

- The black body spectrum of the sun is white light
- Objects hotter than about 500 °C glow visibly
- But even your skin emits invisible thermal radiation



## Radiative Heat Transfer

- Your skin radiates heat at a rate given by the Stefan-Boltzmann law:

$$\text{radiated power} = \text{emissivity} \cdot \text{stefan-boltzmann constant} \cdot \text{temperature}^4 \cdot \text{area}$$

where temperature is an absolute temperature.

- Because of the 4<sup>th</sup> power, thermal radiation is extremely sensitive to temperature.
- Black or gray objects with different temperatures can exchange heat via thermal radiation

## Limiting Thermal Radiation (Part 1)

- Insulation can reduce radiative heat flow by
  - having surfaces with low emissivities
  - reducing temperature differences between surfaces
- Emissivity depends on temperature
  - You can see high-temperature emissivity
    - black surfaces have high-temperature emissivities near 1
    - white, clear, shiny surfaces values near 0
  - You can't see low-temperature emissivity
    - most materials have low-temperature emissivities near 1
    - conducting (metallic) surfaces can have values near 0

## Limiting Thermal Radiation (Part 2)

- To reduce radiative heat flow
  - use conducting, low-emissivity surfaces
  - allow exterior surfaces to reach ambient temperature

## Question 4

- Why do greenhouse gases warm the earth?

## Earth Equilibrium Temperature

- Earth receives thermal radiation from the sun
- Earth emits thermal radiation into space
- Earth's temperature set by balance condition:
  - Earth must emit heat at same rate as it absorbs heat
  - Earth's net radiative heat flow must be zero
  - Balance requires Earth's radiating surface is -18 °C.
- Atmosphere contributes to thermal radiation!
- Radiating surface is 5 km above ground level!

## Effects of the Atmosphere

- Atmosphere has a temperature gradient
  - air expands and cools as its altitude increases
  - air temperature decreases 6.6 °C per km of altitude
- Atmosphere's average temperature
  - at 5 km is -18 °C
  - at ground level is 15 °C

## Effects of Greenhouse Gases

- Greenhouse gases “darken” atmosphere
  - Low-temperature emissivity of atmosphere increases
  - Effective radiating surface moves to higher altitude
  - Average temperature at ground level increases
- Increasing greenhouse gases cause global warming
- Greenhouse gases
  - include H<sub>2</sub>O, CO<sub>2</sub>, nitrogen oxides, and methane
  - don't include N<sub>2</sub> or O<sub>2</sub>, which are transparent to IR
- Limiting greenhouse gases is critical to our future

## Summary about Clothing, Insulation, and Climate

- Clothing and insulation limit heat transfer
- They use materials with low thermal conductivities
- They introduce drag to impede convection
- They use low emissivities to reduce radiation
- Greenhouse gases affect Earth's thermal radiation
- Those gases raise Earth's surface temperature

## Air Conditioners

### Observations about Air Conditioners

- They cool the air in a room
- They emit hot air from their outside vents
- They consume lots of electric power
- They are less efficient on hotter days
- Some can be reversed so that they heat room air

### 5 Questions about Air Conditioners

- Why doesn't heat flow from cold to hot?
- Why does an air conditioner need electricity?
- How does an air conditioner cool room air?
- What role does the electricity play?
- How does an air conditioner heat outdoor air?



## Question 1

- Why doesn't heat flow from cold to hot?
  - Does such heat flow violate the laws of motion?
  - Does such heat flow violate some other laws?

## Laws Governing Heat Flow

- The laws of thermodynamics
  - govern the flow of thermal energy
  - establish relationships between
    - disordered (thermal) energy and ordered energy
    - heat and work

## Law of Thermal Equilibrium

- This law observes that there is a consistency about situations in which heat does not flow:

“If two objects are in thermal equilibrium with a third object, then they are in thermal equilibrium with each other.”

## Law of Conservation of Energy

- This law recognizes that heat is a form of energy:

“The change in the internal energy equals the heat in minus the work out”

- where:
  - The internal energy is thermal + stored energies
  - The heat in is the heat transferred into object
  - The work out is the external work done by object

## Order versus Disorder

- Converting ordered energy into thermal energy
  - involves events that are likely to occur, so it
  - is easy to accomplish and often happens
- Converting thermal energy into ordered energy
  - involves events that are unlikely to occur, so it
  - is hard to accomplish and effectively never happens
- Statistically, ordered always becomes disordered

## Entropy

- Entropy is the measure of an object's disorder
  - Includes both thermal and structural disorders
- An isolated system's entropy never decreases,
- but entropy can move or be transferred
- Entropy is NOT a conserved quantity!

## Law of Entropy

- This law observes that entropy guides the time evolution of isolated systems:

“The entropy of a thermally isolated system never decreases”

## More on the Law of Entropy

- According to the Law of Entropy:
  - Entropy of thermally isolated system can't decrease,
  - but entropy can be redistributed within the system
  - so part of the system can become hotter while another part becomes colder!
- Exporting entropy is like throwing out trash!

## Natural Heat Flow

- One unit of thermal energy is more disordering to a cold object than to a hot object, therefore
- when heat flows from hot object to cold object,
  - the hot object's entropy decreases
  - and the cold object's entropy **increases**,
  - so the overall entropy of the system increases
  - and the total energy is conserved
- Laws of motion and thermodynamics satisfied

## Unnatural Heat Flow

- When heat flows from cold object to hot object,
  - the cold object's entropy **decreases**,
  - and the hot object's entropy **increases**
  - so the overall entropy of the system **decreases**
  - although the total energy is conserved
- The Law of Entropy is violated
  - To save that law, we need more entropy!
  - Something ordered must become disordered!

## Question 2

- Why does an air conditioner need electricity?

## Air Conditioners and Entropy

- Air conditioners
  - move heat from cold room air to hot outside air
  - and would cause entropy to decrease
  - were it not for the electric power they consume!
- Electric energy is ordered,
  - so turning it into thermal energy increases entropy.
- Air conditioner satisfies the Law of Entropy by
  - consuming electric energy (or some other order).

## Heat Machines

- Air conditioners
  - use work to transfer heat from cold to hot
  - are a type of “heat pump”
- Automobiles
  - use flow of heat from hot to cold to do work
  - are a type of “heat engine”
- Heat pumps and heat engines obey the Law of Entropy!

## Air conditioners (Part 1)

- An air conditioner
  - moves heat from cold room air to hot outside air,
  - against its natural flow, therefore
  - it must convert order energy into disordered energy
  - so as not to decrease the world’s total entropy!
- An air conditioner uses a “working fluid” to
  - absorb heat from the cool room air
  - and release heat to the warm outside air

## Air conditioners (Part 2)

- The air conditioner’s indoor evaporator
  - transfers heat from room air to working fluid,
- its outdoor condenser
  - transfers heat from working fluid to outside air
- and its outdoor compressor
  - does work on working fluid and produces entropy.

## Question 3

- How does an air conditioner cool room air?

## The Evaporator (Part 1)

- The evaporator is a long, wide metal pipe,
  - a heat exchanger between air and working fluid.
- The working fluid
  - arrives as a high pressure, room temperature liquid
  - but loses pressure passing through a constriction
  - and enters the evaporator as a low pressure liquid.
- Loss of pressure destabilizes the liquid phase
- The liquid working fluid begins to evaporate!

## The Evaporator (Part 2)

- Working fluid evaporates in the evaporator
  - It needs thermal energy to evaporate,
  - so it absorbs heat from the room air.
- Working fluid leaves the evaporator
  - as a low density gas near room temperature
  - and carries away some of the room’s thermal energy
- Heat has left the room!

### Question 4

- What role does the electricity play?

### The Compressor

- The compressor increases the gas's density
- Working fluid
  - arrives as a low density gas near room temperature,
  - has work done on it by the compressor,
  - and experiences a rise in temperature as a result.
- Working fluid leaves the compressor
  - as a hot, high density gas
  - and carries away electric energy as thermal energy.
- Ordered energy has become disordered energy!

### Question 5

- How does an air conditioner heat outdoor air?

### The Condenser (Part 1)

- The condenser is a long, narrow metal pipe
  - pipe is heat exchanger between air and working fluid
- The working fluid
  - arrives as a hot, high density gas
  - but begins to lose heat to the cooler outdoor air
- Loss of heat destabilizes the gaseous phase,
  - so the gaseous working fluid begins to condense!

### The Condenser (Part 2)

- Working fluid condenses in the condenser
  - It must get rid of thermal energy to condense,
  - so it releases heat into the outside air.
- Working fluid leaves the condenser
  - as high-pressure room-temperature liquid
  - having released some of the room's thermal energy
- Heat has reached the outside air!

### Air Conditioner Overview

- Indoor evaporator
  - transfers heat from room air to working fluid
- Outdoor compressor
  - does work on fluid, raising density and temperature
- Outdoor condenser
  - transfers heat from working fluid to outside air,
    - including thermal energy extracted from inside air
    - and thermal energy added by compressor.

### **Summary about Air Conditioners**

- They pump heat from cold to hot
- They don't violate thermodynamics
- They convert ordered energy to thermal energy

## **Automobiles**

### **Observations about Automobiles**

- They burn gas to obtain their power
- They are rated in horsepower and by volume
- Their engines contain "cylinders"
- They have electrical systems
- They are propelled by their wheels

### **6 Questions about Automobiles**

- How can an automobile run on thermal energy?
- How efficient can an automobile engine be?
- How is an automobile engine a heat engine?
- Why do cars sometime "knock?"
- How is a diesel engine different?
- What about the rest of the automobile?

### **Question 1**

- How can an automobile run on thermal energy?
  - Doesn't the Law of Entropy forbid this conversion?
  - Doesn't burning destroy gasoline's order completely?

### **Heat Engines**

- An automobile engine is a "heat engine"
- A heat engine
  - allows heat to flow naturally from hot to cold
  - but diverts some and converts it into useful work
- Converting heat to work decreases entropy
  - but natural heat flow increases entropy, so
  - some can be converted without decreasing entropy.

## Heat Pumps

- An air conditioner is a “heat pump”
- A heat pump
  - transfers some heat unnaturally from cold to hot
  - while converting useful work into heat
- Unnatural heat flow decreases entropy
  - but converting work to heat increases entropy, so
  - some heat can flow without decreasing entropy.

## Question 2

- How efficient can an automobile engine be?
  - What fraction of thermal energy can become work?

## Efficiency

- Heat engines and pumps are limited by the Law of Entropy
  - They cannot decrease the world’s overall entropy
  - Their efficiencies depend on temperature differences
- As the temperature difference increases,
  - it becomes harder to move heat from cold to hot
  - so a heat pump becomes less efficient,
  - and it becomes easier to move heat from hot to cold
  - so a heat engine becomes more efficient.

## Question 3

- How is an automobile engine a heat engine?

## Internal Combustion Engine

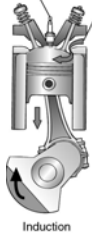
- An internal combustion engine
  - burns fuel and air in an enclosed space
  - to produce hot burned gases.
- As it allows heat to flow to cold outside air
  - it converts some heat into useful work
  - and uses that work to propel a vehicle.

## Four Stroke Engine

- Induction Stroke: fill cylinder with fuel & air
- Compression Stroke: squeeze mixture
- Power Stroke: burn and extract work
- Exhaust Stroke: empty cylinder of exhaust

## Induction Stroke

- Engine pulls piston out of cylinder
- Low pressure inside cylinder
- Atmospheric pressure pushes fuel and air mixture into cylinder
- Engine does work on the gases during this stroke



## Compression Stroke

- Engine pushes piston into cylinder
- Mixture is compressed to high pressure and temperature
- Engine does work on the gases during this stroke



## Power Stroke

- Mixture burns to form hot gases
- Gases push piston out of cylinder
- Gases expand to lower pressure and temperature
- Gases do work on engine during this stroke



## Exhaust Stroke

- Engine pushes piston into cylinder
- High pressure inside cylinder
- Pressure pushes burned gases out of cylinder
- Engine does work on the gases during this stroke



## Ignition System

- Car stores energy in an electromagnet
- Energy is released as a high voltage pulse
- Electric spark ignites fuel and air mixture
- Two basic types of ignition
  - Classic: points and spark coil
  - Electronic: transistors and pulse transformer

## Efficiency Limits

- Even ideal engine isn't perfect
  - Not all the thermal energy can become work
  - Some heat must be ejected into atmosphere
- However, ideal efficiency improves as
  - the burned gases become hotter
  - and the outside air becomes colder.
- Real engines never reach ideal efficiency

### Question 4

- Why do cars sometime “knock?”

### Knocking and Gasolines

- Compressing a gas increases its temperature
- During the compression stroke,
  - the fuel and air mixture becomes extremely hot
  - and that mixture can ignite spontaneously
  - in a process called “knocking” or “preignition”
- To avoid knocking,
  - the car can reduce its compression ratio
  - or increase the ignition resistance of its fuel
- Higher “octane” fuels are simply harder to ignite

### Question 5

- How is a diesel engine different?

### Diesel Engine

- It uses compression heating to ignite fuel
  - It squeeze pure air to high pressure/temperature,
  - injects fuel between compression and power strokes,
  - and fuel burns upon entry into the superheated air
- Power stroke extracts work from burned gases
- Because of its higher compression ratio,
  - its fuel burns to a higher final temperature
  - and the diesel engine has a higher potential efficiency

### Question 6

- What about the rest of the automobile?

### Vehicle Pollution

- Incomplete burning leaves carbon monoxide and hydrocarbons in the exhaust
- Accidental oxidization of nitrogen produces nitrogen oxides in the exhaust
- Diesel exhaust includes many carbonized particulates



## Catalytic Converter

- Platinum assists oxidization of carbon monoxide and hydrocarbons to carbon dioxide and water
- Rhodium assists reduction of nitrogen oxides to nitrogen and oxygen.
- Catalysts supported on high specific surface structure in exhaust duct: catalytic converter

## Transmissions

- Provide mechanical advantage and coupling control between the engine and the wheels
- Two basic types
  - Manual: clutch and gears
  - Automatic: fluid coupling and gears

## Manual Transmission

- Clutch uses friction to convey torque from engine to drive shaft
  - Opening clutch decouples engine and shaft
  - Closing clutch allows engine to twist shaft
- Gears control mechanical advantage

## Automatic Transmission

- Fluid coupling uses moving fluid to convey torque to drive shaft
  - Engine turns impeller (fan) that pushes fluid
  - Moving fluid spins turbine (fan) and drive shaft
  - Decoupling isn't required
- Gears control mechanical advantage

## Brakes

- Use sliding friction to reduce car's energy
- Two basic types
  - Drum: cylindrical drum and curved pads
  - Disk: disk-shaped rotor and flat pads
- Brakes are operated hydraulically
  - Pedal squeezes fluid out of master cylinder
  - Fluid entering slave cylinder activates brake

## Summary about Automobiles

- Cylinders expand hot gas to do work
- Use the flow of heat from hot burned gases to cold atmosphere to produce work
- Energy efficiency is limited by thermodynamics
- Higher temperatures increase efficiency

# Clocks

## Observations About Clocks

- They divide time into uniform intervals
- They measure time by counting those intervals
- Some clocks use motion to mark their intervals
- Others clocks don't appear to involve motion
- They require energy to operate
- They have good but not perfect accuracy

## 4 Questions about Clocks

- Why don't any modern clocks use hourglasses?
- Are all repetitive motions equally accurate?
- Why are some watches more accurate?
- How do clocks use harmonic oscillators?

## Question 1

- Why don't any modern clocks use hourglasses?


## Non-Repetitive Motions: Timers

- Devices that measure a single interval of time,
  - sandglasses,
  - water clocks,
  - and candles
- are fine as timers and were common in antiquity.
- They are poorly suited to subdividing the day
  - because they require frequent operator intervention
  - and that operator requirement limits their accuracy.

## Repetitive Motions: Clocks

- Devices that tick off time intervals repetitively
  - pendulums,
  - torsion balances,
  - and tuning forks
- began appearing in clocks about 500 years ago.
- They are well suited to subdividing the day
  - because they require no operator intervention
  - and their ticks can be counted mechanically.

## About Repetitive Motions

- A device with a stable equilibrium
  - will move repetitively about that equilibrium, 
  - as long as it has excess energy.
- That repetitive motion sets a clock's accuracy,
  - so it mustn't depend on externals such as
    - the temperature, air pressure, or time of day,
    - the clock's store of energy,
    - or the mechanism that observes the motion.

## Question 2

- Are all repetitive motions equally accurate?



## Some Specifics

- A little terminology
  - Period: time of full repetitive motion cycle
  - Frequency: cycles completed per unit of time
  - Amplitude: peak distance away from motion's center
- An important application of that terminology
  - In an ideal clock, the repetitive motion's period shouldn't depend on its amplitude

## Harmonic Oscillators (Part 1)

- A harmonic oscillator
  - has a stable equilibrium
  - and a restoring force that's proportional to displacement from that equilibrium.
- Its period is independent of its amplitude.
- At a conceptual level, it always has
  - an inertial aspect (e.g., a mass)
  - and a springlike restoring force aspect (e.g., a spring).

## Harmonic Oscillators (Part 2)

- The period of a harmonic oscillator decreases as
  - the mass aspect becomes smaller
  - and the springlike aspect becomes stiffer
- Common harmonic oscillators include
  - a mass on a spring (the prototypical form) 
  - a pendulum 
  - a flagpole
  - a tuning fork

## Question 3

- Why are some watches more accurate?

## The Limits to the Accuracy

- Clocks exhibit practical limits:
  - Sustaining motion can influence the period
  - Observing the period can influence the period
  - Sensitivity to temperature, pressure, wind, ...
- Clocks also exhibit fundamental limits:
  - Oscillation decay limits preciseness of period

## Question 4

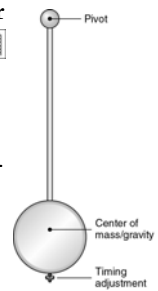
- How do clocks use harmonic oscillators?

## Pendulums

- A pendulum is (almost) a harmonic oscillator
  - Its period is proportional to  $(\text{length}/\text{gravity})^{1/2}$
  - and its period is (almost) independent of amplitude.

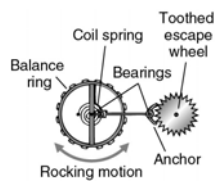
## Pendulum Clocks

- Pendulum is the clock's timekeeper
- For accuracy, the pendulum's
  - pivot-to-center-of-gravity distance is
    - temperature stabilized
    - and adjustable for variations in gravity.
  - It is streamlined to minimize air drag.
  - Its motion is sustained gently
  - and measured gently.
- The clock mustn't move or tilt.



## Balance Ring Clocks

- A torsional spring causes a balance-ring harmonic oscillator to twist back and forth.
- Gravity exerts no torque about the ring's pivot and therefore has no influence on the period.
- Twisting is sustained and measured with minimal effects on the ring's motion.

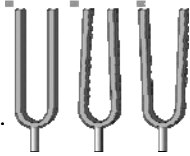


## Quartz Oscillators

- Crystalline quartz is a harmonic oscillator
  - The crystal's mass provides the inertial aspect
  - and its body provides the springlike aspect.
- Quartz's oscillation decay is extremely slow
  - so its fundamental accuracy is very high.
- Quartz is piezoelectric
  - Its mechanical and electrical changes are coupled, so
  - its motion can be induced and measured electrically.

## Quartz Clocks

- The quartz tuning fork is excited electronically.
- The clock counts the vibrations electronically.
- The period of those vibrations is insensitive to gravity, temperature, pressure, and acceleration.
- Quartz's slow vibration decay gives it a very precise period.
- The crystal's tuning-fork shape yields a slow, efficient vibration.



## Summary about Clocks

- Most clocks involve harmonic oscillators
- Amplitude independence aids accuracy
- Clock sustains and counts oscillations
- Oscillators that lose little energy work best

## Musical Instruments

### Observations about Musical Instruments

- They can produce different notes
- They must be tuned to produce the right notes
- They sound different, even on the same note
- They require energy to create sound

### 6 Questions about Musical Instruments

- Why do strings produce specific notes?
- Why does a vibrating string sound like a string?
- How does bowing cause a string to vibrate?
- Why do stringed instruments need surfaces?
- What is vibrating in a wind instrument?
- Why does a drum sound particularly different?

### Question 1

- Why do strings produce specific notes?



## Oscillations of a Taut String

- A taut string has
  - a mass that provides its inertial aspect,
  - a tension that provides its springlike aspect,
  - a stable equilibrium shape (straight line),
  - and restoring forces proportional to displacement.
- A taut string is a harmonic oscillator
  - that oscillates about its equilibrium shape
  - with a pitch independent of amplitude (i.e., volume)!

## A Taut String's Pitch

- A string's springlike aspect stiffness is set by
  - its tension and
  - its length (which determines its curvature).
- The string's inertial aspect is set by
  - its mass.


## Fundamental Vibration

- A string has a fundamental vibrational mode
  - in which it vibrates as a single arc, up and down,
  - with a displacement antinode at its center
  - and a displacement node at each of its two ends. 
- Its fundamental pitch (frequency of vibration) is
  - proportional to  $\text{tension}^{1/2}$ ,
  - proportional to  $1/\text{length}$ , and
  - proportional to  $1/\text{mass}^{1/2}$ . 


## Question 2

- Why does a vibrating string sound like a string?

## A String's Harmonics (Part 1)

- A string can also vibrate as
  - two half-strings (one extra antinode),
  - three third-strings (two extra antinodes), and so on.
- These higher-order vibrational modes
  - have pitches higher than the fundamental mode
  - and are called "overtones."
- Overtones with pitches that are integer multiples of the fundamental pitch are called "harmonics."
- A string's overtones are all harmonics! 


## A String's Harmonics (Part 2)

- First overtone involves two half-strings
  - Twice the fundamental pitch: 2<sup>nd</sup> harmonic
  - One octave above the fundamental frequency
- Second overtone involves three third-strings
  - Three times the fundamental pitch: 3<sup>rd</sup> harmonic
  - An octave and a fifth above the fundamental
- Bowing or plucking a string excites a mixture of fundamental and harmonic vibrations, giving the string its characteristic sound 

### Question 3

- How does bowing cause a string to vibrate?


### Plucking and Bowing

- Plucking a string transfers energy instantly
- Bowing a string transfers energy gradually
  - by doing a little work on the string every cycle
  - so that excess energy builds up gradually.
  - This gradual buildup is resonant energy transfer.
- The string will vibrate sympathetically when
  - another object vibrates at its resonant frequency
  - and it gradually extracts energy from that object. 

### Question 4

- Why do stringed instruments need surfaces?

### Projecting Sound

- In air, sound consists of density fluctuations
  - Air has a stable equilibrium: uniform density
  - Disturbances from uniform density make air vibrate
- Vibrating strings barely project sound because
  - air flows around thin vibrating objects
  - and is only slightly compressed or rarefied.
- Surfaces project sound much better because
  - air can't flow around surfaces easily
  - and is substantially compressed or rarefied. 

### Question 5

- What is vibrating in a wind instrument?

### Oscillations of Air in a Tube

- Air in a tube has
  - mass that provides its inertial aspect,
  - pressures that provide its springlike aspect,
  - a stable equilibrium structure (uniform density),
  - and restoring forces proportional to displacement.
- Air in a tube is a harmonic oscillator
  - that oscillates about its equilibrium shape
  - with a pitch independent of amplitude (i.e., volume)!

### Air in a Tube's Pitch

- Air column's springlike aspect stiffness is set by
  - its pressure and
  - its length (which determines its pressure gradient).
- Air column's inertial aspect is set by
  - its mass.

### Fundamental Vibration Open-Open Column

- The air column vibrates as a single object
  - with a pressure antinode at the middle of the column
  - and a pressure node at each of the two open ends.
- Its fundamental pitch (frequency of vibration) is
  - proportional to pressure<sup>1/2</sup>,
  - proportional to 1/length, and
  - proportional to 1/density<sup>1/2</sup>.

### Fundamental Vibration Open-Closed Column

- The air column vibrates as a single object
  - with a pressure antinode at the closed end
  - and a pressure node at the open end.
- The air column in an open-closed pipe vibrates
  - like half the air column in an open-open pipe
  - and at half the frequency of an open-open pipe.

### Air Harmonics (Part 1)

- In an open-open pipe, the overtones are at
  - twice the fundamental (two pressure antinodes),
  - three times the fundamental (three antinodes),
  - and so on (all integer multiples or "harmonics").
- In an open-closed pipe, the overtones are at
  - three times the fundamental (two antinodes),
  - five times the fundamental (three antinodes),
  - and so on (all odd integer multiples or "harmonics").

### Air Harmonics (Part 2)

- Blowing across the column tends to excite a mixture of fundamental and harmonic vibrations
- Examples
  - Organ pipes
  - Recorders
  - Flutes
  - Whistles
- Reeds and horns also use a vibrating air column

### Question 6

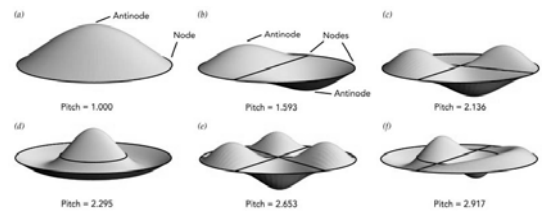
- Why does a drum sound particularly different?



## Surface Instruments

- Most 1-dimensional instruments
  - are harmonic oscillators
  - that can vibrate at half, third, quarter length, etc.
  - and have harmonic overtones.
- Most 2- or 3- dimensional instruments
  - are harmonic oscillators
  - that have complicated higher-order vibrations
  - and have non-harmonic overtones.
- Examples: drums, cymbals, bells

## Drumhead Vibrations



## Summary of Musical Instrument

- They use strings, air, etc. as harmonic oscillators
- Pitches are independent of amplitude/volume
- Tuned by tension/pressure, length, density
- Often have harmonic overtones
- Project vibrations into the air as sound

## The Sea

## Observations about the Sea

- The sea is rarely calm; it is covered with waves
- The broadest waves travel fastest
- Waves seem to get steeper near shore
- Waves break or crumble near shore
- Waves bend gradually toward the shore

## 5 Questions about the Sea

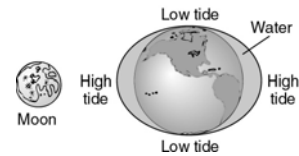
- Why are there tides?
- How do giant tides develop?
- How does water in a wave move?
- How is a tsunami different from normal waves?
- Why do waves bend and break near shore?

## Question 1

- Why are there tides?

## The Tides (Part 1)

- The moon's gravity acts on the earth,
- but the moon's gravity is nonuniform
- so the earth's oceans are pulled out of round
- and two tidal bulges form on opposite sides.

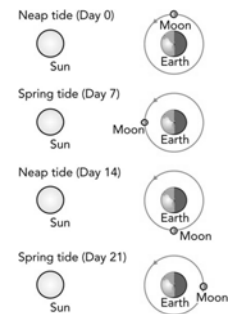


## The Tides (Part 2)

- These bulges move as the earth rotates, so
  - each shore experiences almost two high tides per day
  - and almost two low tides per day.
- The heights of these tides vary with latitude.
  - They are strongest near equator
  - and weakest near poles.

## The Sun's Influence

- Sun's gravity affects the tides
- Strongest tides are when moon and sun are aligned
- Weakest tides are when moon and sun are at right angles

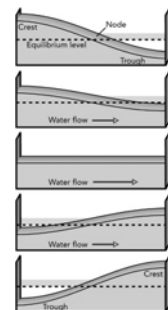


## Question 2

- How do giant tides develop?

## Tidal Resonance

- Water in a confined channel can slosh back and forth
  - It has a stable equilibrium (level)
    - and it experiences springlike forces.
- It's another harmonic oscillator
- Its period depends on its inertia and its stiffness
- If the sloshing time matches the tidal period, resonance occurs



## Standing and Traveling Waves

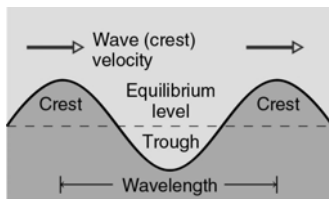
- Sloshing involves standing waves
  - Water in a finite container has standing wave modes,
    - with nodes and antinodes that remain stationary.
- Open water surf involves traveling waves
  - Water in an infinite sea has traveling wave modes,
    - with crests and troughs that move continuously.

## Question 3

- How does water in a wave move?

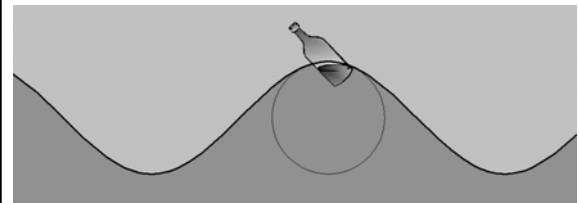
## Water Waves

- Sloshing involves deep water waves: all of the water moves back and forth
- Surface waves affect only water near the surface



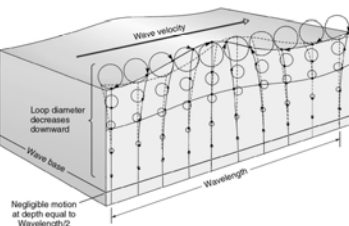
## Water's Motion (Part 1)

- Only the wave structure travels across the water.
- Surface water itself circles as the wave passes.
- The wave's crests are formed from local water.



## Water's Motion (Part 2)

- The circling is strongest at the surface,
- and becomes weak about  $1/2$  wavelength deep.



## Question 4

- How is a tsunami different from normal waves?

## Waves and Wavelength

- The longer the wavelength of surface wave,
  - the faster it travels,
  - the deeper it extends into the water,
  - and the more power it conveys for its amplitude.
- Tsunamis are
  - very long wavelength, deep, and powerful waves.
  - They are also not strictly surface waves.

## Question 5

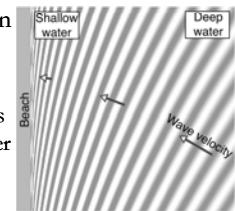
- Why do waves bend and break near shore?

## Breaking Waves

- Shallow water distorts a wave's circling motion.
- As the water grows shallower, a surface wave
  - slows down and its wavelength decreases.
  - Its crests grow taller and more tightly bunched.
- Waves break when the water can't form a crest
- The slope of the seabed affects breaking
  - If the seabed slopes gradually, there is rolling surf
  - If the seabed slopes sharply, plunging breakers occur

## Changing Wave Speeds

- Waves experience reflection
  - Changes in wave speed cause partial reflection
  - and the bigger the speed change, the more reflection
- Waves experience refraction
  - Changes in wave speed can redirect the wave
  - Waves bend toward shore as they slow in shallowing water



## Summary of the Sea

- The moon's gravity causes the tides
- The tides can cause resonant motion in channels
- Tidal resonances are standing waves
- The open sea exhibits traveling waves
- Water moves in circles in those waves
- Waves break when the water gets too shallow